Q.1 A boy’s catapult is made of rubber cord which is 42 cm long, with 6 mm diameter of cross-section and of negligible mass. The boy keeps a stone weighing 0.02 kg on it and stretches the cord by 20 cm by applying a constant force. When released, the stone flies off with a velocity of 20 ms\(^{-1}\). Neglect the change in the area of cross-section of the cord while stretched. The Young’s modulus of rubber is closest to:

Options 1. \(10^6\) Nm\(^{-2}\) ✓
2. \(10^4\) Nm\(^{-2}\)
3. \(10^8\) Nm\(^{-2}\)
4. \(10^3\) Nm\(^{-2}\)

Q.2 A thermally insulated vessel contains 150 g of water at 0°C. Then the air from the vessel is pumped out adiabatically. A fraction of water turns into ice and the rest evaporates at 0°C itself. The mass of evaporated water will be closest to:

(Latent heat of vaporization of water = \(2.10 \times 10^6\) J kg\(^{-1}\) and Latent heat of Fusion of water = \(3.36 \times 10^5\) J kg\(^{-1}\))

Options 1. 35 g
2. 20 g  ✔
3. 130 g
4. 150 g

Q. 3
A 20 Henry inductor coil is connected to a 10 ohm resistance in series as shown in figure. The time at which rate of dissipation of energy (Joule's heat) across resistance is equal to the rate at which magnetic energy is stored in the inductor, is:

\[ E = \frac{10 \, \Omega}{20 \, \text{H}} \]

Options
1. \( \frac{1}{2} \ln 2 \)
2. \( 2 \ln 2 \)  ✔
3. \( \frac{2}{\ln 2} \)
4. \( \ln 2 \)

Q. 4
Radiation coming from transitions \( n=2 \) to \( n=1 \) of hydrogen atoms fall on He\(^+\) ions in \( n=1 \) and \( n=2 \) states. The possible transition of helium ions as they absorb energy from the radiation is:

Options
1. \( n=2 \rightarrow n=3 \)
2. \( n=2 \rightarrow n=4 \)  ✔
3. \( n=2 \rightarrow n=5 \)
4. \( n = 1 \rightarrow n = 4 \)

Q.5 Four identical particles of mass M are located at the corners of a square of side 'a'. What should be their speed if each of them revolves under the influence of others' gravitational field in a circular orbit circumscribing the square?

Options

1. \( 1.35 \sqrt{\frac{GM}{a}} \)
2. \( 1.21 \sqrt{\frac{GM}{a}} \)
3. \( 1.41 \sqrt{\frac{GM}{a}} \)
4. \( 1.16 \sqrt{\frac{GM}{a}} \) ✓

Q.6 The wavelength of the carrier waves in a modern optical fiber communication network is close to:

Options

1. 2400 nm
2. 900 nm
3. 600 nm
4. 1500 nm ✓
Q.7 A thin circular plate of mass $M$ and radius $R$ has its density varying as $\rho(r) = \rho_0 r$ with $\rho_0$ as constant and $r$ is the distance from its center. The moment of Inertia of the circular plate about an axis perpendicular to the plate and passing through its edge is $I = a MR^2$. The value of the coefficient $a$ is:

Options
1. $\frac{3}{5}$
2. $\frac{1}{2}$
3. $\frac{8}{5}$ ✓
4. $\frac{3}{2}$

Q.8 An alternating voltage $v(t) = 220 \sin 100\pi t$ volt is applied to a purely resistive load of $50\Omega$. The time taken for the current to rise from half of the peak value to the peak value is:

Options
1. 7.2 ms
2. 5 ms
3. 2.2 ms
4. 3.3 ms ✓
Q.9  The bob of a simple pendulum has mass 2 g and a charge of 5.0 μC. It is at rest in a uniform horizontal electric field of intensity 2000 V/m. At equilibrium, the angle that the pendulum makes with the vertical is:
(take g = 10 m/s^2)

Options
1. \( \tan^{-1} (0.2) \)
2. \( \tan^{-1} (2.0) \)
3. \( \tan^{-1} (0.5) \)  \( \checkmark \)
4. \( \tan^{-1} (5.0) \)

Q.10  A circular coil having \( N \) turns and radius \( r \) carries a current \( I \). It is held in the XZ plane in a magnetic field \( \hat{B} \). The torque on the coil due to the magnetic field is:

Options
1. \( B \pi r^2 I N \)  \( \checkmark \)
2. \( \frac{Br^2 I}{\pi N} \)
3. \( \frac{B\pi r^2 I}{N} \)
4. Zero
Two identical beakers A and B contain equal volumes of two different liquids at 60°C each and left to cool down. Liquid in A has density of $8 \times 10^2$ kg/m$^3$ and specific heat of 2000 J kg$^{-1}$ K$^{-1}$ while liquid in B has density of $10^3$ kg m$^{-3}$ and specific heat of 4000 J kg$^{-1}$ K$^{-1}$. Which of the following best describes their temperature versus time graph schematically? (assume the emissivity of both the beakers to be the same)

Options

1. ![Graph 1](60°C, T, A, B, t →)

2. ![Graph 2](60°C, T, B, A, t →) ✓

3. ![Graph 3](60°C, T, A and B, t →)

4. ![Graph 4](60°C, T, A, B, t →)

Q.12 If $10^{22}$ gas molecules each of mass $10^{-26}$ kg collide with a surface (perpendicular to it) elastically per second over an area 1 m$^2$ with a speed $10^4$ m/s, the pressure exerted by the gas molecules will be of the order of:

Options

1. $10^4$ N/m$^2$
2. $10^{16}$ N/m²
3. $10^8$ N/m²
4. $10^3$ N/m²  ✓

Question Type: MCQ  
Question ID: 41652912706  
Option 1 ID: 41652949603  
Option 2 ID: 41652949605  
Option 3 ID: 41652949604  
Option 4 ID: 41652949602  
Status: Not Answered  
Chosen Option: --

Q.13  For the circuit shown, with $R_1 = 1.0 \ \Omega$, $R_2 = 2.0 \ \Omega$, $E_1 = 2 \ \text{V}$ and $E_2 = E_3 = 4 \ \text{V}$, the potential difference between the points 'a' and 'b' is approximately (in V):

![Circuit Diagram]

Options 1. 3.3  ✓  
2. 2.3  
3. 2.7  
4. 3.7

Question Type: MCQ  
Question ID: 41652912712  
Option 1 ID: 41652949627  
Option 2 ID: 41652949629  
Option 3 ID: 41652949628  
Option 4 ID: 41652949626  
Status: Not Answered  
Chosen Option: --

Q.14  A plane electromagnetic wave travels in free space along the $x$-direction. The electric field component of the wave at a particular point of space and time is $E = 6 \ \text{V/m}$ along $y$-direction. Its corresponding magnetic field component, $B$ would be:

Options 1. $2 \times 10^{-8}$ T along $z$-direction  ✓  
2. $2 \times 10^{-8}$ T along $y$-direction
3. $6 \times 10^{-8} \text{T along } z\text{-direction}$

4. $6 \times 10^{-8} \text{T along } x\text{-direction}$

**Q.15**

In figure, the optical fiber is $l=2 \text{ m long}$ and has a diameter of $d=20 \mu \text{m}$. If a ray of light is incident on one end of the fiber at angle $\theta_1 = 40^\circ$, the number of reflections it makes before emerging from the other end is close to:

(refractive index of fiber is 1.31 and $\sin 40^\circ = 0.64$)

![Diagram of optical fiber with incident and emergent rays]

Options 1. 55000
2. 57000 ✓
3. 45000
4. 66000

**Q.16**

Two particles move at right angle to each other. Their de Broglie wavelengths are $\lambda_1$ and $\lambda_2$ respectively. The particles suffer perfectly *inelastic* collision. The de Broglie wavelength $\lambda$, of the final particle, is given by:

Options
1. \[ \frac{2}{\lambda} = \frac{1}{\lambda_1} + \frac{1}{\lambda_2} \]
2. \[ \lambda = \frac{\lambda_1 + \lambda_2}{2} \]
3. \[ \lambda = \sqrt{\lambda_1 \lambda_2} \]
4. \[ \frac{1}{\lambda^2} = \frac{1}{\lambda_1^2} + \frac{1}{\lambda_2^2} \quad \checkmark \]

**Q.17** The reverse breakdown voltage of a Zener diode is 5.6 V in the given circuit.

![Circuit Diagram]

The current \( I_Z \) through the Zener is:

Options
1. 10 mA \( \checkmark \)
2. 7 mA
3. 17 mA
4. 15 mA

**Q.18** An upright object is placed at a distance of 40 cm in front of a convergent lens of focal length 20 cm. A convergent mirror of focal length 10 cm is placed at a distance of 60 cm on the other side of the lens. The position and size of the final image will be:
In an interference experiment the ratio of amplitudes of coherent waves is \( \frac{a_1}{a_2} = \frac{1}{3} \).

The ratio of maximum and minimum intensities of fringes will be:

Options
1. 4 \( \checkmark \)
2. 9
3. 2
4. 18
Four particles A, B, C and D with masses \( m_A = m, \) \( m_B = 2m, \) \( m_C = 3m \) and \( m_D = 4m \) are at the corners of a square. They have accelerations of equal magnitude with directions as shown. The acceleration of the centre of mass of the particles is:

\[
\begin{align*}
\mathbf{a} & \overset{\text{1.}}{=} \frac{\mathbf{a}}{5} (\mathbf{i} + \mathbf{j}) \\
\mathbf{a} & \overset{\text{2.}}{=} \frac{\mathbf{a}}{5} (\mathbf{i} - \mathbf{j}) \quad \checkmark \\
\mathbf{a} & \overset{\text{3.}}{=} \frac{\mathbf{a}}{5} (\mathbf{i} + \mathbf{j}) \\
\mathbf{a} & \overset{\text{4.}}{=} \text{Zero}
\end{align*}
\]

Q.21
A 200 \( \Omega \) resistor has a certain color code. If one replaces the red color by green in the code, the new resistance will be:

Options

1. 300 \( \Omega \)
2. 100 \( \Omega \)
3. 400 \( \Omega \)
4. 500 \( \Omega \)  \( \checkmark \)
Q.22  A thin strip 10 cm long is on a U shaped wire of negligible resistance and it is connected to a spring of spring constant 0.5 Nm⁻¹ (see figure). The assembly is kept in a uniform magnetic field of 0.1 T. If the strip is pulled from its equilibrium position and released, the number of oscillations it performs before its amplitude decreases by a factor of e is N. If the mass of the strip is 50 grams, its resistance 10 Ω and air drag negligible, N will be close to:

Options
1. 1000
2. 5000 ✓
3. 10000
4. 50000

Q.23  A steel wire having a radius of 2.0 mm, carrying a load of 4 kg, is hanging from a ceiling. Given that g = 3.1 m s⁻², what will be the tensile stress that would be developed in the wire?

Options
1. $5.2 \times 10^6$ Nm⁻²
2. $6.2 \times 10^6$ Nm⁻²
3. $4.8 \times 10^6$ Nm⁻²
4. $3.1 \times 10^6$ Nm⁻² ✓
Q.24  Ship A is sailing towards north-east with velocity \( \vec{v} = 30 \hat{i} + 50 \hat{j} \) km/hr where \( \hat{i} \) points east and \( \hat{j} \), north. Ship B is at a distance of 80 km east and 150 km north of Ship A and is sailing towards west at 10 km/hr. A will be at minimum distance from B in:

Options  
1. 4.2 hrs.  
2. 3.2 hrs.  
3. 2.6 hrs. \( \checkmark \)  
4. 2.2 hrs.

---

Q.25  A wire of length 2L is made by joining two wires A and B of same length but different radii r and 2r and made of the same material. It is vibrating at a frequency such that the joint of the two wires forms a node. If the number of antinodes in wire A is p and that in B is q then the ratio p : q is:

Options  
1. 3 : 5  
2. 4 : 9  
3. 1 : 4  
4. 1 : 2 \( \checkmark \)

---

Question Type: MCQ  
Question ID: 41652912697  
Option 1 ID: 41652949566  
Option 2 ID: 41652949569  
Option 3 ID: 41652949568  
Option 4 ID: 41652949567  
Status: Not Answered  
Chosen Option: --

Question Type: MCQ  
Question ID: 41652912708  
Option 1 ID: 41652949611  
Option 2 ID: 41652949612  
Option 3 ID: 41652949613  
Option 4 ID: 41652949610  
Status: Answered  
Chosen Option: 4
Q.26
A solid conducting sphere, having a charge \( Q \), is surrounded by an uncharged conducting hollow spherical shell. Let the potential difference between the surface of the solid sphere and that of the outer surface of the hollow shell be \( V \). If the shell is now given a charge of \(-4 \, Q\), the new potential difference between the same two surfaces is:

Options
1. \(-2 \, V\)
2. \(2 \, V\)
3. \(V\) \(\checkmark\)
4. \(4 \, V\)

Q.27
Water from a pipe is coming at a rate of 100 liters per minute. If the radius of the pipe is 5 cm, the Reynolds number for the flow is of the order of: (density of water = 1000 kg/m³, coefficient of viscosity of water = 1 mPa s)

Options
1. \(10^2\)
2. \(10^4\) \(\checkmark\)
3. \(10^3\)
4. \(10^6\)

Q.28
In SI units, the dimensions of \( \sqrt{\frac{\varepsilon_0}{\mu_0}} \) is:

Options
1. \(AT^2M^{-1}L^{-1}\)
2. $A^{2}T^{3}M^{-1}L^{-2}$ ✓
3. $A^{-1}TML^{3}$
4. $AT^{-3}ML^{3/2}$

Q.29 Voltage rating of a parallel plate capacitor is 500 V. Its dielectric can withstand a maximum electric field of $10^{6}$ V/m. The plate area is $10^{-4}$ m$^2$. What is the dielectric constant if the capacitance is 15 pF?

(given $\varepsilon_0 = 8.86 \times 10^{-12}$ C$^2$/Nm$^2$)

Options 1. 3.8
2. 8.5 ✓
3. 4.5
4. 6.2

Q.30 A particle moves in one dimension from rest under the influence of a force that varies with the distance travelled by the particle as shown in the figure. The kinetic energy of the particle after it has travelled 3 m is:

![Graph showing force vs. distance with force values at 1, 2, and 3 N at distances 1, 2, and 3 m respectively.]

Question Type: MCQ
Question ID: 41652912696
Option 1 ID: 41652949562
Option 2 ID: 41652949563
Option 3 ID: 41652949564
Option 4 ID: 41652949565
Status: Answered
Chosen Option: 2

Question Type: MCQ
Question ID: 41652912711
Option 1 ID: 41652949623
Option 2 ID: 41652949625
Option 3 ID: 41652949624
Option 4 ID: 41652949622
Status: Not Answered
Chosen Option: --
Q.1 The quantum number of four electrons are given below:
I. \( n = 4, l = 2, m_l = -2, m_s = -\frac{1}{2} \)
II. \( n = 3, l = 2, m_l = 1, m_s = +\frac{1}{2} \)
III. \( n = 4, l = 1, m_l = 0, m_s = +\frac{1}{2} \)
IV. \( n = 3, l = 1, m_l = 1, m_s = -\frac{1}{2} \)
The correct order of their increasing energies will be:

Options 1. \( I < III < II < IV \)  
2. \( IV < II < III < I \)  \(\checkmark\)  
3. \( I < II < III < IV \)  
4. \( IV < III < II < I \)  

Q.2 An organic compound neither reacts with neutral ferric chloride solution nor with Fehling solution. It however, reacts with Grignard reagent and gives positive iodoform test. The compound is:

Options
Q.3 Maltose on treatment with dilute HCl gives:

Options:
1. D-Glucose ✓
2. D-Fructose
3. D-Galactose
4. D-Glucose and D-Fructose
For silver, $C_p(J K^{-1} \text{ mol}^{-1}) = 23 + 0.01T$. If the temperature $(T)$ of 3 moles of silver is raised from 300 K to 1000 K at 1 atm pressure, the value of $\Delta H$ will be close to:

- 1. 16 kJ
- 2. 62 kJ
- 3. 13 kJ
- 4. 21 kJ

Q.5 The major product of the following reaction is:

$$\text{Conc HBr (excess) heat}$$

Options

1. 

| Br-CH\(_2\)CH\(_3\) |

2. 

| OH |

$\text{CH}_2\text{CH}_2\text{Br}$

3. 

| Br |

$\text{Br}-\text{CHCH}_3$

4. 

$\text{CH}_2\text{CH}_2\text{Br}$
Q.6 The IUPAC name of the following compound is:

\[
\begin{align*}
\text{CH}_3 & \quad \text{OH} \\
\text{H}_3\text{C} & \quad \text{CH} \quad \text{CH} \quad \text{CH}_2 \quad \text{COOH}
\end{align*}
\]

Options
1. 4-Methyl-3-hydroxypentanoic acid
2. 4,4-Dimethyl-3-hydroxybutanoic acid
3. 2-Methyl-3-hydroxypentan-5-oic acid
4. 3-Hydroxy-4-methylpentanoic acid

Q.7 Which of the following amines can be prepared by Gabriel phthalimide reaction?

Options
1. t-butyramine
2. n-butyramine ✔
3. triethylamine
4. neo-pentylamine

Q.8 Coupling of benzene diazonium chloride with 1-naphthol in alkaline medium will give:

Options
Q.9
The major product of the following reaction is:

\[
\text{Br} \quad \xrightarrow{\text{NaBH}_4, \text{MeOH, } 25^\circ\text{C}} \quad \text{O}
\]

Options
1. 
2. 
3. 
4. 

Chosen Option: 1

Q.10
An organic compound 'X' showing the following solubility profile is:

- Insoluble in water
- Insoluble in 5% HCl
- Soluble in 10% NaOH
- Insoluble in 10% NaHCO₃

Options
1. m-Cresol
2. o-Toluidine
3. Oleic acid

Chosen Option: m-Cresol
4. Benzamide

Q.11
100 mL of a water sample contains 0.81 g of calcium bicarbonate and 0.73 g of magnesium bicarbonate. The hardness of this water sample expressed in terms of equivalents of CaCO₃ is:
(molar mass of calcium bicarbonate is 162 g mol⁻¹ and magnesium bicarbonate is 146 g mol⁻¹)

Options
1. 100 ppm
2. 1,000 ppm
3. 5,000 ppm
4. 10,000 ppm √

Q.12
Diborane (B₂H₆) reacts independently with O₂ and H₂O to produce, respectively:

Options
1. HBO₂ and H₃BO₃
2. H₃BO₃ and B₂O₃
3. B₂O₃ and [BH₄]⁻
4. B₂O₃ and H₃BO₃ √
Q.13  The size of the iso-electronic species Cl\(^-\), Ar and Ca\(^{2+}\) is affected by:

Options
1. nuclear charge
   ✓
2. azimuthal quantum number of valence shell
3. electron-electron interaction in the outer orbitals
4. Principal quantum number of valence shell

Q.14  Element ‘B’ forms ccp structure and ‘A’ occupies half of the octahedral voids, while oxygen atoms occupy all the tetrahedral voids. The structure of bimetallic oxide is:

Options
1. A\(_2\)BO\(_4\)
2. AB\(_2\)O\(_4\)
   ✓
3. A\(_2\)B\(_2\)O
4. A\(_4\)B\(_2\)O

Q.15  With respect to an ore, Ellingham diagram helps to predict the feasibility of its

Options
1. Electrolysis
2. Zone refining
3. Vapour phase refining
4. Thermal reduction ✓

Q.16

For the reaction 2A + B → C, the values of initial rate at different reactant concentrations are given in the table below. The rate law for the reaction is:

<table>
<thead>
<tr>
<th>[A] (mol L⁻¹)</th>
<th>[B] (mol L⁻¹)</th>
<th>Initial Rate (mol L⁻¹s⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.05</td>
<td>0.05</td>
<td>0.045</td>
</tr>
<tr>
<td>0.10</td>
<td>0.05</td>
<td>0.090</td>
</tr>
<tr>
<td>0.20</td>
<td>0.10</td>
<td>0.72</td>
</tr>
</tbody>
</table>

Options
1. Rate = k[A]²[B]
2. Rate = k[A]³[B]
3. Rate = k[A][B]
4. Rate = k[A][B]² ✓

Q.17

The correct order of the spin-only magnetic moment of metal ions in the following low-spin complexes, [V(CN)₆]⁴⁻, [Fe(CN)₆]⁴⁻, [Ru(NH₃)₆]³⁺, and [Cr(NH₃)₆]²⁺, is:

Options
1. V²⁺ > Cr²⁺ > Ru³⁺ > Fe²⁺ ✓
2. Cr²⁺ > V²⁺ > Ru³⁺ > Fe²⁺
3. Cr²⁺ > Ru³⁺ > Fe²⁺ > V²⁺
4. V²⁺ > Ru³⁺ > Cr²⁺ > Fe²⁺
Q.18 Adsorption of a gas follows Freundlich adsorption isotherm. \( x \) is the mass of the gas adsorbed on mass \( m \) of the adsorbent.

The plot of \( \log \frac{x}{m} \) versus \( \log p \) is shown in the given graph. \( \frac{x}{m} \) is proportional to:

\[
\begin{align*}
\text{Options} & \quad 1. \quad p^3 \\
& \quad 2. \quad p^2 \\
& \quad 3. \quad p^{2/3} \quad \checkmark \\
& \quad 4. \quad p^{3/2}
\end{align*}
\]

Q.19 Which is wrong with respect to our responsibility as a human being to protect our environment?

Options 1. Using plastic bags. \( \checkmark \)

2. Restricting the use of vehicles
3. Avoiding the use of floodlighted facilities.
4. Setting up compost tin in gardens.
Q.20  In order to oxidise a mixture of one mole of each of FeC_2O_4, Fe_2(C_2O_4)_3, FeSO_4 and Fe_2(SO_4)_3 in acidic medium, the number of moles of KMnO_4 required is:

Options
1. 1
2. 2 √
3. 3
4. 1.5

Q.21  Given that E_{O_2/H_2O} = +1.23 V;
E_{S_2O_8^{2-}/SO_4^{2-}} = 2.05 V
E_{Br_2/Br^-} = +1.09 V;
E_{Au^{3+}/Au} = +1.4 V

The strongest oxidising agent is:

Options
1. O_2
2. S_2O_8^{2-} √
3. Br_2
4. Au^{3+}
Q.22 The lanthanide ion that would show colour is:
Options 1. Lu$^{3+}$
2. La$^{3+}$
3. Gd$^{3+}$
4. Sm$^{3+}$ ✓

Q.23 In the following compounds, the decreasing order of basic strength will be:
Options 1. C$_2$H$_5$NH$_2$ > NH$_3$ > (C$_2$H$_5$)$_2$NH
2. (C$_2$H$_5$)$_2$NH > NH$_3$ > C$_2$H$_5$NH$_2$
3. NH$_3$ > C$_2$H$_5$NH$_2$ > (C$_2$H$_5$)$_2$NH
4. (C$_2$H$_5$)$_2$NH > C$_2$H$_5$NH$_2$ > NH$_3$ ✓

Q.24 Assertion: Ozone is destroyed by CFCs in the upper stratosphere.
Reason: Ozone holes increase the amount of UV radiation reaching the earth.
Options Assertion and reason are correct, but the reason is not the explanation for the assertion.
2. Assertion is false, but the reason is correct.
3. Assertion and reason are incorrect.
Assertion and reason are both correct, and the reason is the correct explanation for the assertion.

Q.25 The following ligand is:

Options 1. tridentate
2. hexadentate
3. bidentate
4. tetradentate

Q.26 The correct order of hydration enthalpies of alkali metal ions is:

Options 1. Na\(^+\) > Li\(^+\) > K\(^+\) > Rb\(^+\) > Cs\(^+\)
2. Na\(^+\) > Li\(^+\) > K\(^+\) > Cs\(^+\) > Rb\(^+\)
3. Li\(^+\) > Na\(^+\) > K\(^+\) > Rb\(^+\) > Cs\(^+\)
4. Li\(^+\) > Na\(^+\) > K\(^+\) > Cs\(^+\) > Rb\(^+\)
Q.27  Which one of the following equations does not correctly represent the first law of thermodynamics for the given processes involving an ideal gas? (Assume non-expansion work is zero)

Options:
1. Isochoric process: $\Delta U = q$
2. Isothermal process: $q = -w$
3. Cyclic process: $q = -w$
4. Adiabatic process: $\Delta U = -w$  ✔

Q.28  The major product of the following reaction is:

\[
\text{O} \quad \text{Cl} \\
\begin{array}{c}
\text{O} + \text{Ph} \\
\text{Cl}
\end{array} \\
\text{(i) AlCl}_3, \text{heat} \\
\text{H}_2\text{O}
\]

Options:
1. 
2. ✔
3. 

Q.29 The vapour pressures of pure liquids A and B are 400 and 600 mmHg, respectively at 298 K. On mixing the two liquids, the sum of their initial volumes is equal to the volume of the final mixture. The mole fraction of liquid B is 0.5 in the mixture. The vapour pressure of the final solution, the mole fractions of components A and B in vapour phase, respectively are:

Options
1. 500 mmHg, 0.5, 0.5
2. 450 mmHg, 0.4, 0.6
3. 450 mmHg, 0.5, 0.5
4. 500 mmHg, 0.4, 0.6  ✓

Q.30 If solubility product of $\text{Zr}_3(\text{PO}_4)_4$ is denoted by $K_{sp}$ and its molar solubility is denoted by $S$, then which of the following relation between $S$ and $K_{sp}$ is correct?

Options
1. $S = \left(\frac{K_{sp}}{144}\right)^{1/6}$
2. $S = \left( \frac{K_{sp}}{6912} \right)^{1/6}$

3. $S = \left( \frac{K_{sp}}{629} \right)^{1/6}$

4. $S = \left( \frac{K_{sp}}{216} \right)^{1/6}$

Section: Mathematics

**Q.1**

The length of the perpendicular from the point $(2, -1, 4)$ on the straight line,

$$\frac{x + 3}{10} = \frac{y - 2}{-7} = \frac{z}{1}$$

is:

Options
1. greater than 3 but less than 4
2. greater than 4
3. less than 2
4. greater than 2 but less than 3

**Q.2**

The shortest distance between the line $y = x$ and the curve $y^2 = x - 2$ is:

Options
1. $\frac{7}{4\sqrt{2}}$
2. $\frac{7}{8}$
3. $\frac{11}{4\sqrt{2}}$
4. 2
Q.3 Let \( y = y(x) \) be the solution of the differential equation, 
\[
(x^2 + 1)^2 \frac{dy}{dx} + 2x(x^2 + 1)y = 1
\]
that \( y(0) = 0 \). If \( \sqrt{a} \ y(1) = \frac{\pi}{32} \), then the value of ‘a’ is:

Options
1. \( \frac{1}{16} \)
2. \( \frac{1}{2} \)
3. \( \frac{1}{4} \)
4. 1

Q.4 All possible numbers are formed using the digits 1, 1, 2, 2, 2, 2, 3, 4, 4 taken all at a time. The number of such numbers in which the odd digits occupy even places is:

Options
1. 175
2. 162
3. 180
4. 160
Q.5

If \( \alpha = \cos^{-1}\left(\frac{3}{5}\right) \), \( \beta = \tan^{-1}\left(\frac{1}{3}\right) \), where

\( 0 < \alpha, \beta < \frac{\pi}{2} \), then \( \alpha - \beta \) is equal to:

Options

1. \( \tan^{-1}\left(\frac{9}{14}\right) \)
2. \( \cos^{-1}\left(\frac{9}{5\sqrt{10}}\right) \)
3. \( \sin^{-1}\left(\frac{9}{5\sqrt{10}}\right) \)
4. \( \tan^{-1}\left(\frac{9}{5\sqrt{10}}\right) \)

Chosen Option : 3

Q.6

If \( f(x) = \log_{e}\left(\frac{1-x}{1+x}\right) \), \(|x| < 1\), then

\( f\left(\frac{2x}{1+x^2}\right) \) is equal to:

Options

1. \((f(x))^2\)
2. \(2f(x^2)\)
3. \(-2f(x)\)
4. \(2f(x)\)

Chosen Option : 3

Q.7
The equation of a plane containing the line of intersection of the planes $2x - y - 4 = 0$ and $y + 2z - 4 = 0$ and passing through the point $(1, 1, 0)$ is:

Options
1. $x - 3y - 2z = -2$
2. $x + 3y + z = 4$
3. $x - y - z = 0 \checkmark$
4. $2x - z = 2$

Q.8 If $S_1$ and $S_2$ are respectively the sets of local minimum and local maximum points of the function, $f(x) = 9x^4 + 12x^3 - 36x^2 + 25$, $x \in \mathbb{R}$, then:

Options
1. $S_1 = \{-2\}; S_2 = \{0, 1\}$
2. $S_1 = \{-1\}; S_2 = \{0, 2\}$
3. $S_1 = \{-2, 0\}; S_2 = \{1\}$
4. $S_1 = \{-2, 1\}; S_2 = \{0\} \checkmark$

Q.9 If

$$2y = \left(\cot^{-1}\left(\frac{\sqrt{3} \cos x + \sin x}{\cos x - \sqrt{3} \sin x}\right)\right)^2, x \in \left[0, \frac{\pi}{2}\right]$$

then $\frac{dy}{dx}$ is equal to:

Options
1. $\frac{\pi}{6} - x$
2. $2x - \frac{\pi}{3}$
3. $x - \frac{\pi}{6} \checkmark$
4. \[ \frac{\pi}{3} - x \]

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Option 2 ID: 41652949845  
Option 3 ID: 41652949844  
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Status: Answered  
Chosen Option: 3

Q.10  
The magnitude of the projection of the vector \( \hat{2i} + 3\hat{j} + \hat{k} \) on the vector perpendicular to the plane containing the vectors \( \hat{i} + \hat{j} + \hat{k} \) and \( \hat{i} + 2\hat{j} + 3\hat{k} \), is:

Options  
1. \( 3\sqrt{6} \)  
2. \( \frac{\sqrt{3}}{2} \)  
3. \( \frac{\sqrt{6}}{2} \)  
4. \( \frac{\sqrt{3}}{2} \)  

Q.11  
Let \( A = \begin{pmatrix} \cos\alpha & -\sin\alpha \\ \sin\alpha & \cos\alpha \end{pmatrix}, (\alpha \in \mathbb{R}) \) such that 
\[ A^{32} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}. \] Then a value of \( \alpha \) is:

Options  
1. 0  
2. \( \frac{\pi}{16} \)  
3. \( \frac{\pi}{64} \)  
4. \( \frac{\pi}{32} \)
Q.12  A point on the straight line, $3x + 5y = 15$ which is equidistant from the coordinate axes will lie only in:

Options
1. $1^{st}$ and $2^{nd}$ quadrants  $\checkmark$
2. $1^{st}$, $2^{nd}$ and $4^{th}$ quadrants
3. $1^{st}$ quadrant
4. $4^{th}$ quadrant

Q.13  \[
\int \frac{\sin \frac{5x}{2}}{\sin \frac{x}{2}} \, dx \text{ is equal to:}
\]
(where $c$ is a constant of integration.)

Options
1. $x + 2 \sin x + \sin 2x + c$  $\checkmark$
2. $2x + \sin x + \sin 2x + c$
3. $x + 2 \sin x + 2 \sin 2x + c$
4. $2x + \sin x + 2 \sin 2x + c$

Q.14  Let $O(0, 0)$ and $A(0, 1)$ be two fixed points. Then the locus of a point $P$ such that the perimeter of $\triangle AOP$ is 4, is:

Options
1. $8x^2 + 9y^2 - 9y = 18$
2. $9x^2 - 8y^2 + 8y = 16$
3. $8x^2 - 9y^2 + 9y = 18$
4. $9x^2 + 8y^2 - 8y = 16 \checkmark$

**Q.15**

If $\cos(\alpha + \beta) = \frac{3}{5}$, $\sin(\alpha - \beta) = \frac{5}{13}$ and $0 < \alpha, \beta < \frac{\pi}{4}$, then $\tan(2\alpha)$ is equal to:

Options:
1. $\frac{21}{16}$
2. $\frac{63}{52}$
3. $\frac{33}{52}$
4. $\frac{63}{16} \checkmark$

**Q.16**

The sum of the squares of the lengths of the chords intercepted on the circle, $x^2 + y^2 = 16$, by the lines, $x + y = n$, $n \in \mathbb{N}$, where $\mathbb{N}$ is the set of all natural numbers, is:

Options:
1. 210 \checkmark
2. 105
3. 320
4. 160
Q.17
\[ \lim_{x \to 0} \frac{\sin^2 x}{\sqrt{2} - \sqrt{1 + \cos x}} \]
equals:

Options
1. \(4\sqrt{2} \quad \checkmark\)
2. \(2\sqrt{2}\)
3. \(\sqrt{2}\)
4. \(4\)

Q.18
The mean and variance of seven observations are 8 and 16, respectively. If 5 of the observations are 2, 4, 10, 12, 14, then the product of the remaining two observations is:

Options
1. 48 \(\checkmark\)
2. 45
3. 49
4. 40

Q.19
Let A and B be two non-null events such that \(A \subset B\). Then, which of the following statements is always correct?

Options
1. \(P(A|B) \geq P(A) \quad \checkmark\)
2. \(P(A|B) = P(B) - P(A)\)
3. \(P(A|B) \leq P(A)\)
4. \(P(A|B) = 1\)
Q.20 The sum of all natural numbers `n` such that 100 < n < 200 and H.C.F. (91, n) > 1 is :

Options 1. 3203
2. 3221
3. 3121 ✅
4. 3303

Q.21 The sum of the co-efficients of all even degree terms in x in the expansion of

\[(x + \sqrt{x^3 - 1})^6 + (x - \sqrt{x^3 - 1})^6, (x > 1)\]

is equal to :

Options 1. 26
2. 32
3. 24 ✅
4. 29

Q.22 The area (in sq.units) of the region

\[A = \{(x, y) \in R \times R | 0 \leq x \leq 3, 0 \leq y \leq 4, y \leq x^2 + 3x\}\]

is :

Options 1. \(\frac{26}{3}\)
2. 8
3. \[\frac{53}{6}\]
4. \[\frac{59}{6}\] √

Q.23 The greatest value of \(c \in \mathbb{R}\) for which the system of linear equations
\[\begin{align*}
  x - cy - cz &= 0 \\
  cx - y + cz &= 0 \\
  cx + cy - z &= 0
\end{align*}\]
has a non-trivial solution, is:

Options 1. \(-1\)
2. \(2\)
3. \(\frac{1}{2}\) √
4. \(0\)

Q.24 The sum of the series
\[2 \cdot 20C_0 + 5 \cdot 20C_1 + 8 \cdot 20C_2 + 11 \cdot 20C_3 + \ldots + 62 \cdot 20C_{20}\]
is equal to:

Options 1. \(2^{26}\)
2. \(2^{25}\) √
3. \(2^{24}\)
4. \(2^{23}\)
Q.25

If \( f(x) = \frac{2 - x \cos x}{2 + x \cos x} \) and \( g(x) = \log_e x \), \( (x > 0) \) then the value of the integral
\[
\int_{\frac{\pi}{4}}^{\frac{\pi}{4}} g(f(x)) \, dx
\]
is:

Options
1. \( \log_e e \)
2. \( \log_e 2 \)
3. \( \log_e 1 \) \( \checkmark \)
4. \( \log_e 3 \)

Q.26

The contrapositive of the statement “If you are born in India, then you are a citizen of India”, is:

Options
1. If you are not born in India, then you are not a citizen of India.
2. If you are a citizen of India, then you are born in India.
3. If you are born in India, then you are not a citizen of India.
4. If you are not a citizen of India, then you are not born in India. \( \checkmark \)

Q.27

The sum of the solutions of the equation
\[
|\sqrt{x} - 2| + \sqrt{x} (\sqrt{x} - 4) + 2 = 0, \quad (x > 0)
\]
is equal to:

Options
1. 10 ✓
2. 9
3. 12
4. 4

Q.28 If \( \alpha \) and \( \beta \) be the roots of the equation \( x^2 - 2x + 2 = 0 \), then the least value of \( n \) for which \( \left( \frac{\alpha}{\beta} \right)^n = 1 \) is:

Options
1. 5
2. 4 ✓
3. 2
4. 3

Q.29 If the tangents on the ellipse \( 4x^2 + y^2 = 8 \) at the points \((1, 2)\) and \((a, b)\) are perpendicular to each other, then \( a^2 \) is equal to:

Options
1. \( \frac{2}{17} \) ✓
2. \( \frac{4}{17} \)
3. \( \frac{64}{17} \)
4. \( \frac{128}{17} \)
Q.30 Let $f : [0, 2] \to \mathbb{R}$ be a twice differentiable function such that $f''(x) > 0$, for all $x \in (0, 2)$. If $\phi(x) = f(x) + f(2 - x)$, then $\phi$ is:

**Options**

1. decreasing on $(0, 2)$
2. increasing on $(0, 2)$
3. increasing on $(0, 1)$ and decreasing on $(1, 2)$.
4. decreasing on $(0, 1)$ and increasing on $(1, 2)$.  
   \[ \checkmark \]