







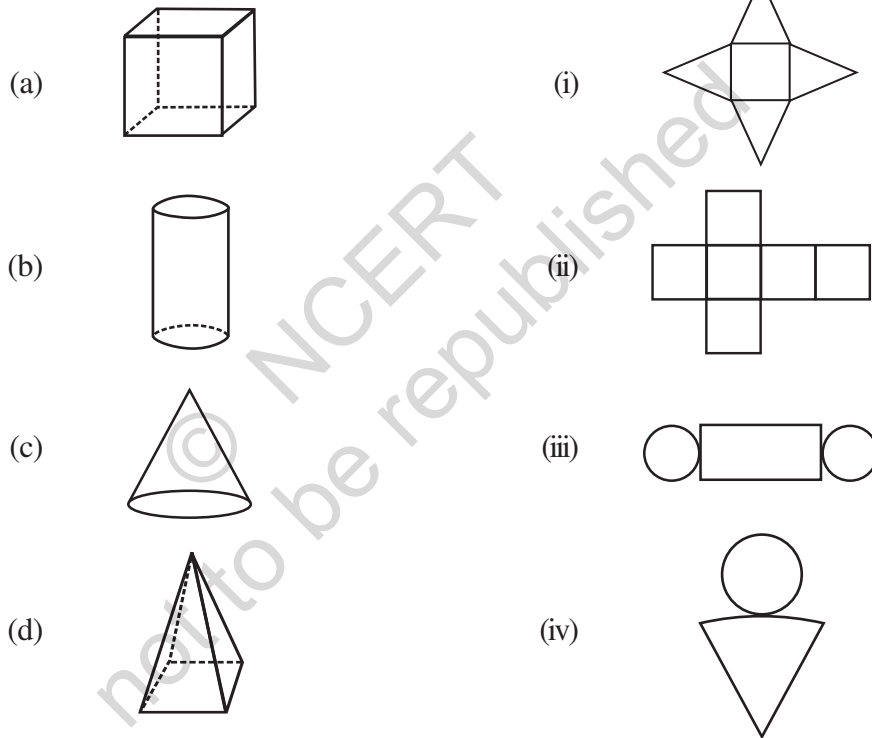




4. Here is an incomplete net for making a cube. Complete it in at least two different ways. Remember that a cube has six faces. How many are there in the net here? (Give two separate diagrams. If you like, you may use a squared sheet for easy manipulation.)



5. Match the nets with appropriate solids:



### Play this game

You and your friend sit back-to-back. One of you reads out a net to make a 3-D shape, while the other attempts to copy it and sketch or build the described 3-D object.

## 15.4 DRAWING SOLIDS ON A FLAT SURFACE

Your drawing surface is paper, which is flat. When you draw a solid shape, the images are somewhat distorted to make them appear three-dimensional. It is a visual illusion. You will find here two techniques to help you.

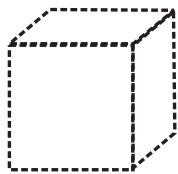


Fig 15.11

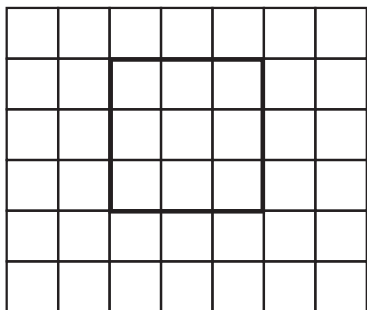
### 15.4.1 Oblique Sketches

Here is a picture of a cube (Fig 15.11). It gives a clear idea of how the cube looks like, when seen from the front. You do not see certain faces. In the drawn picture, the lengths

are not equal, as they should be in a cube. Still, you are able to recognise it as a cube. Such a sketch of a solid is called an **oblique sketch**.

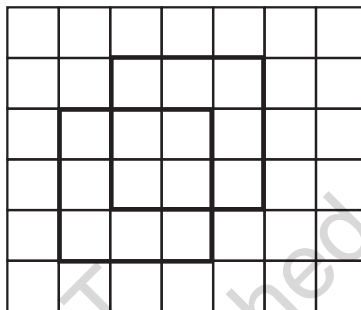
How can you draw such sketches? Let us attempt to learn the technique.

You need a squared (lines or dots) paper. Initially practising to draw on these sheets will later make it easy to sketch them on a plain sheet (without the aid of squared lines or dots!) Let us attempt to draw an oblique sketch of a  $3 \times 3 \times 3$  (each edge is 3 units) cube (Fig 15.12).



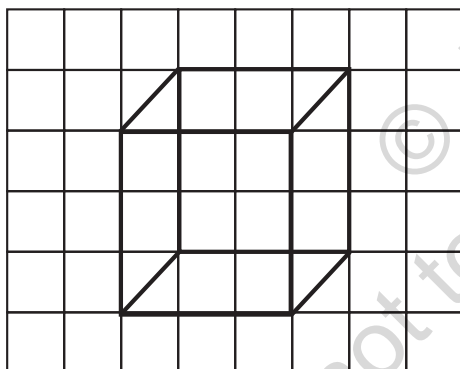
**Step 1**

Draw the **front** face.



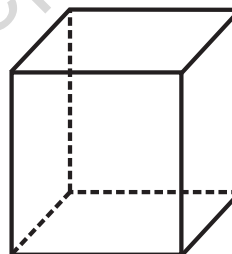
**Step 2**

Draw the **opposite** face. Sizes of the faces have to be same, but the sketch is somewhat off-set from step 1.



**Step 3**

Join the corresponding corners



**Step 4**

Redraw using dotted lines for hidden edges. (It is a convention)  
The sketch is ready now.

**Fig 15.12**

In the oblique sketch above, did you note the following?

- (i) The sizes of the front faces and its opposite are same; and
- (ii) The edges, which are all equal in a cube, appear so in the sketch, though the actual measures of edges are not taken so.

You could now try to make an oblique sketch of a cuboid (remember the faces in this case are rectangles)

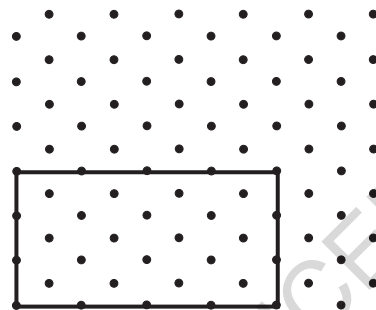
**Note:** You can draw sketches in which measurements also agree with those of a given solid. To do this we need what is known as an **isometric sheet**. Let us try to

make a cuboid with dimensions 4 cm length, 3 cm breadth and 3 cm height on given isometric sheet.

### 15.4.2 Isometric Sketches

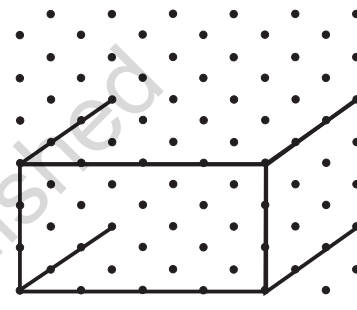
Have you seen an isometric dot sheet? (A sample is given at the end of the book). Such a sheet divides the paper into small equilateral triangles made up of dots or lines. *To draw sketches in which measurements also agree with those of the solid*, we can use isometric dot sheets. [Given on inside of the back cover (3rd cover page).]

Let us attempt to draw an isometric sketch of a cuboid of dimensions  $4 \times 3 \times 3$  (which means the edges forming length, breadth and height are 4, 3, 3 units respectively) (Fig 15.13).



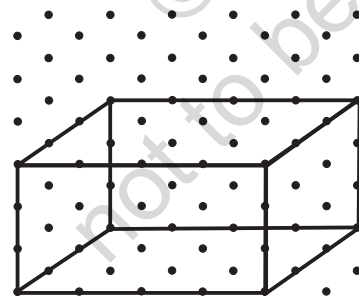
**Step 1**

*Draw a rectangle to show the front face.*



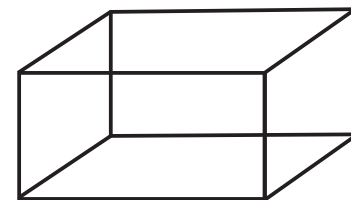
**Step 2**

*Draw four parallel line segments of length 3 starting from the four corners of the rectangle.*



**Step 3**

*Connect the matching corners with appropriate line segments.*



**Step 4**

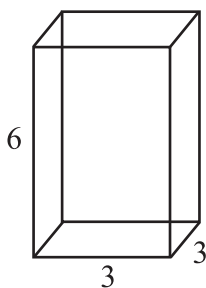
*This is an isometric sketch of the cuboid.*

**Fig 15.13**

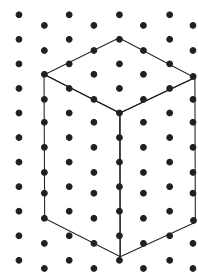
Note that the measurements are of exact size in an isometric sketch; this is not so in the case of an oblique sketch.

**EXAMPLE 1** Here is an oblique sketch of a cuboid [Fig 15.14(i)]. Draw an isometric sketch that matches this drawing.

**SOLUTION** Here is the solution [Fig 15.14(ii)]. Note how the measurements are taken care of.



**Fig 15.14 (i)**



**Fig 15.14 (ii)**

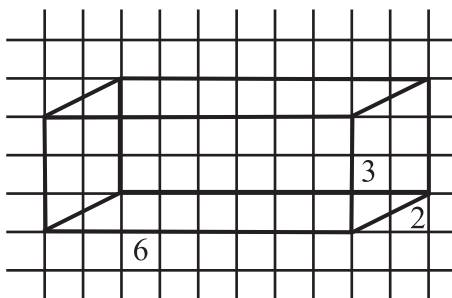


How many units have you taken along (i) 'length'? (ii) 'breadth'? (iii) 'height'? Do they match with the units mentioned in the oblique sketch?

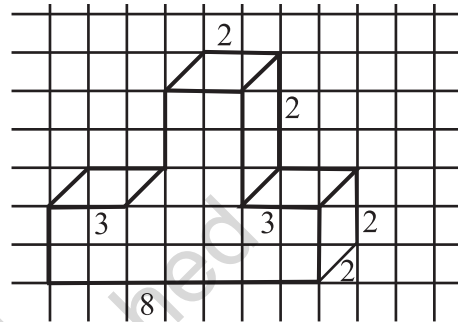
**EXERCISE 15.2**



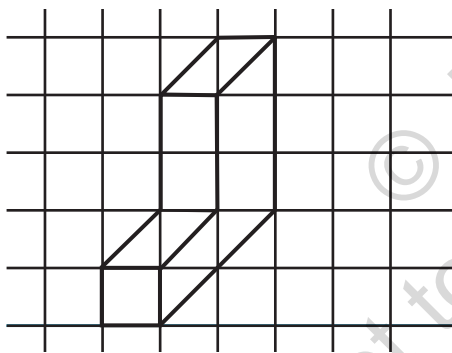
1. Use isometric dot paper and make an isometric sketch for each one of the given shapes:



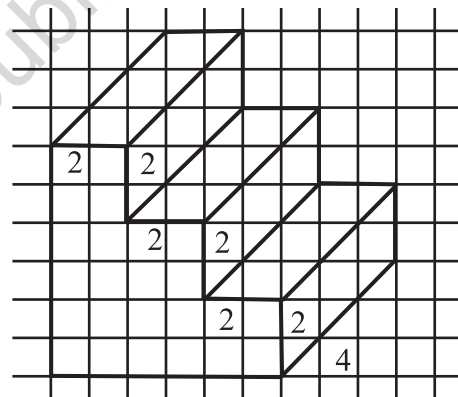
(i)



(ii)



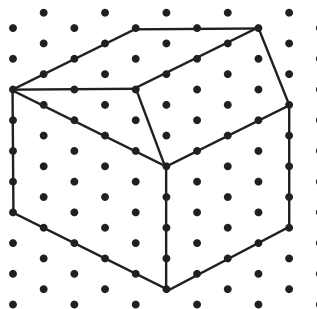
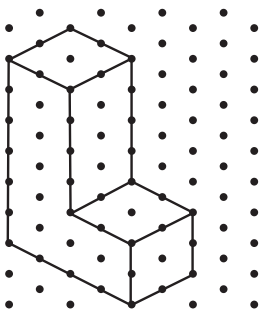
(iii)



(iv)

Fig 15.15

2. The dimensions of a cuboid are 5 cm, 3 cm and 2 cm. Draw three different isometric sketches of this cuboid.
3. Three cubes each with 2 cm edge are placed side by side to form a cuboid. Sketch an oblique or isometric sketch of this cuboid.
4. Make an oblique sketch for each one of the given isometric shapes:

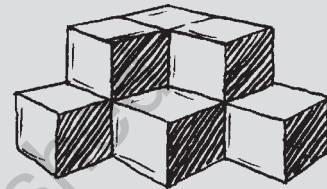
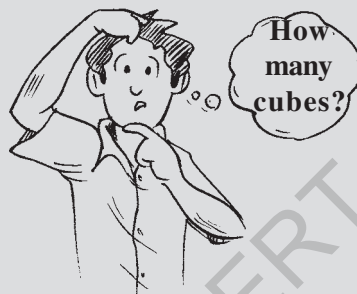


5. Give (i) an oblique sketch and (ii) an isometric sketch for each of the following:
- A cuboid of dimensions 5 cm, 3 cm and 2 cm. (Is your sketch unique?)
  - A cube with an edge 4 cm long.

An isometric sheet is attached at the end of the book. You could try to make on it some cubes or cuboids of dimensions specified by your friend.

### 15.4.3 Visualising Solid Objects

#### Do This



Sometimes when you look at combined shapes, some of them may be hidden from your view.

Here are some activities you could try in your free time to help you visualise some solid objects and how they look. Take some cubes and arrange them as shown in Fig 15.16.

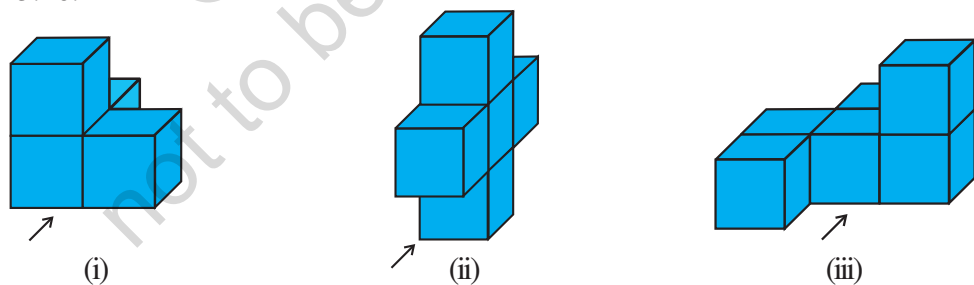


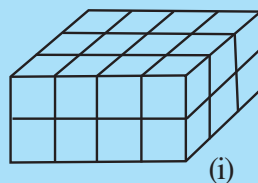
Fig 15.16

Now ask your friend to guess how many cubes there are when observed from the view shown by the arrow mark.

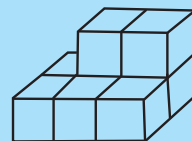
#### TRY THESE



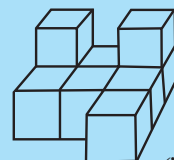
Try to guess the number of cubes in the following arrangements (Fig 15.17).



(i)



(ii)



(iii)

Fig 15.17

Such visualisation is very helpful. Suppose you form a cuboid by joining such cubes. You will be able to guess what the length, breadth and height of the cuboid would be.

**EXAMPLE 2** If two cubes of dimensions 2 cm by 2 cm by 2 cm are placed side by side, what would the dimensions of the resulting cuboid be?

**SOLUTION** As you can see (Fig 15.18) when kept side by side, the length is the only measurement which increases, it becomes  $2 + 2 = 4$  cm.

The breadth = 2 cm and the height = 2 cm.

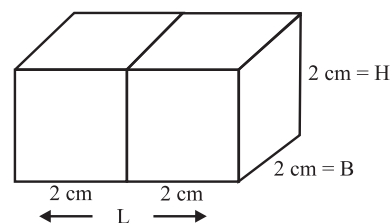


Fig 15.18

### TRY THESE

1. Two dice are placed side by side as shown: Can you say what the total would be on the face opposite to

- (a)  $5 + 6$                       (b)  $4 + 3$

(Remember that in a die sum of numbers on opposite faces is 7)

2. Three cubes each with 2 cm edge are placed side by side to form a cuboid. Try to make an oblique sketch and say what could be its length, breadth and height.

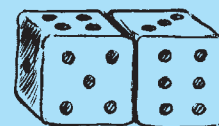


Fig 15.19

## 15.5 VIEWING DIFFERENT SECTIONS OF A SOLID

Now let us see how an object which is in 3-D can be viewed in different ways.

### 15.5.1 One Way to View an Object is by Cutting or Slicing

#### Slicing game

Here is a loaf of bread (Fig 15.20). It is like a cuboid with a square face. You 'slice' it with a knife.

When you give a 'vertical' cut, you get several pieces, as shown in the Figure 15.20. Each face of the piece is a square! We call this face a '**cross-section**' of the whole bread. The cross section is nearly a square in this case.

Beware! If your cut is not 'vertical' you may get a different cross section! Think about it. The boundary of the cross-section you obtain is a plane curve. Do you notice it?

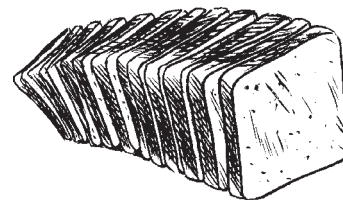


Fig 15.20

#### A kitchen play

Have you noticed cross-sections of some vegetables when they are cut for the purposes of cooking in the kitchen? Observe the various slices and get aware of the shapes that result as cross-sections.

**Play this**

Make clay (or plasticine) models of the following solids and make vertical or horizontal cuts. Draw rough sketches of the cross-sections you obtain. Name them wherever you can.

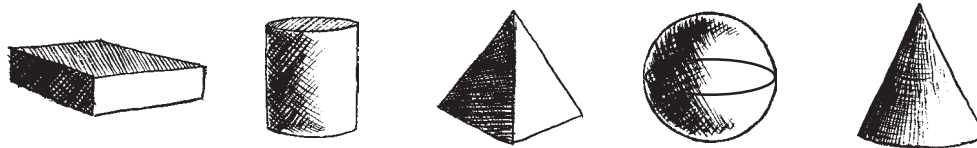


Fig 15.21

**EXERCISE 15.3**

1. What cross-sections do you get when you give a

- (i) vertical cut                      (ii) horizontal cut

to the following solids?

- (a) A brick                      (b) A round apple                      (c) A die  
(d) A circular pipe                      (e) An ice cream cone

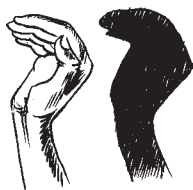


Fig 15.22

**15.5.2 Another Way is by Shadow Play****A shadow play**

Shadows are a good way to illustrate how three-dimensional objects can be viewed in two dimensions. Have you seen a **shadow play**? It is a form of entertainment using solid articulated figures in front of an illuminated back-drop to create the illusion of moving images. It makes some indirect use of ideas in Mathematics.

You will need a source of light and a few solid shapes for this activity. (If you have an overhead projector, place the solid under the lamp and do these investigations.)

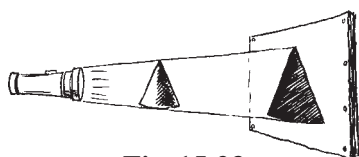


Fig 15.23

Keep a torchlight, *right in front of* a Cone. What type of shadow does it cast on the screen? (Fig 15.23)

The solid is three-dimensional; what is the dimension of the shadow?

If, instead of a cone, you place a cube in the above game, what type of shadow will you get?

Experiment with different positions of the source of light and with different positions of the solid object. Study their effects on the shapes and sizes of the shadows you get.

Here is another funny experiment that you might have tried already: Place a circular plate in the open when the Sun at the noon time is just *right above* it as shown in Fig 15.24 (i). What is the shadow that you obtain?



(i)

Will it be same during



(a) forenoons?

(b) evenings?

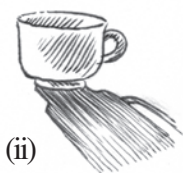


Fig 15.24 (i) - (iii)

Study the shadows in relation to the position of the Sun and the time of observation.

**EXERCISE 15.4**

1. A bulb is kept burning just right above the following solids. Name the shape of the shadows obtained in each case. Attempt to give a rough sketch of the shadow. (You may try to experiment first and then answer these questions).



A ball

(i)



A cylindrical pipe

(ii)



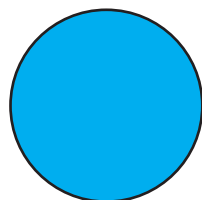
A book

(iii)



2. Here are the shadows of some 3-D objects, when seen under the lamp of an overhead projector. Identify the solid(s) that match each shadow. (There may be multiple answers for these!)

A circle



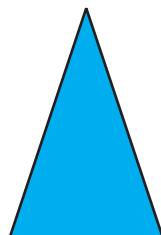
(i)

A square



(ii)

A triangle



(iii)

A rectangle



(iv)

3. Examine if the following are true statements:
- The cube can cast a shadow in the shape of a rectangle.
  - The cube can cast a shadow in the shape of a hexagon.

### 15.5.3 A Third Way is by Looking at it from Certain Angles to Get Different Views

One can look at an object standing in front of it or by the side of it or from above. Each time one will get a different view (Fig 15.25).

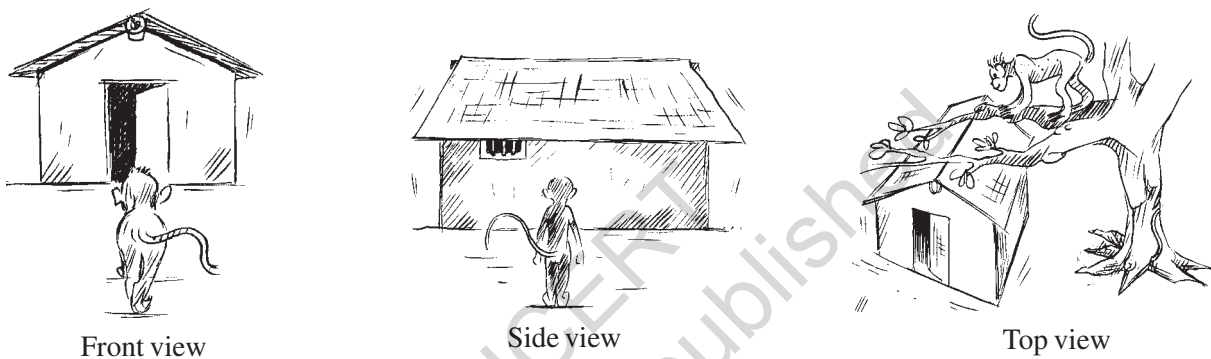


Fig 15.25

Here is an example of how one gets different views of a given building. (Fig 15.26)

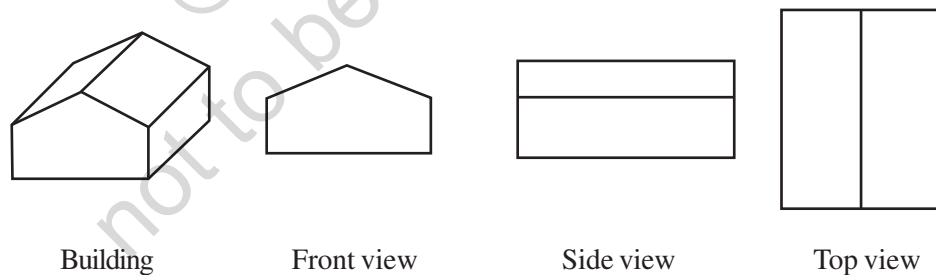


Fig 15.26

You could do this for figures made by joining cubes.

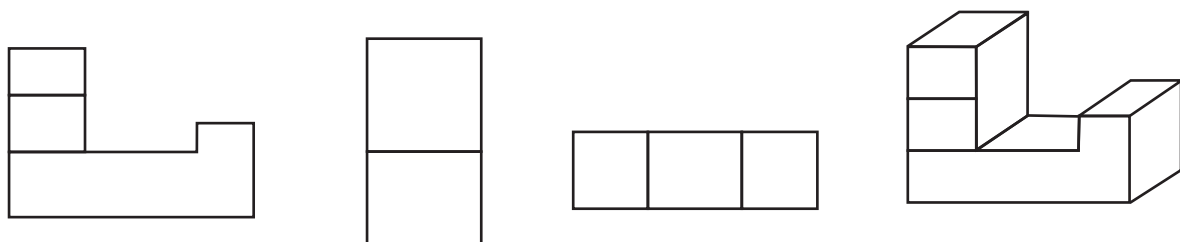
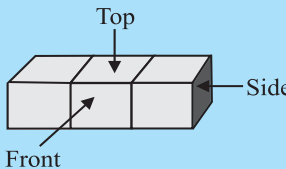



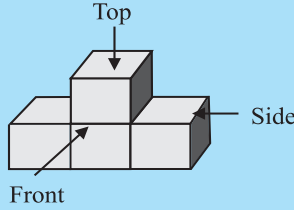


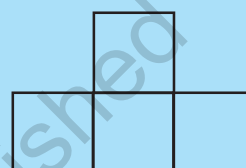
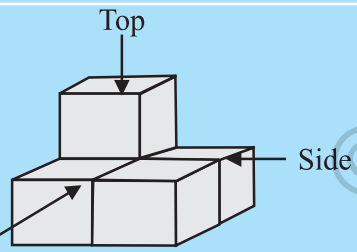
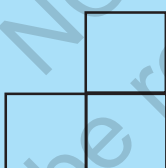
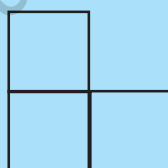
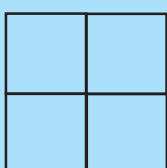
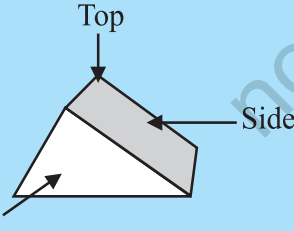





Fig 15.27


Try putting cubes together and then making such sketches from different sides.

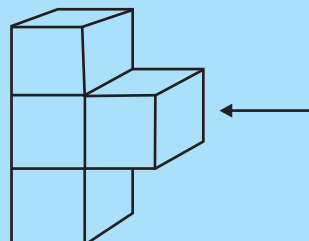
**TRY THESE**

1. For each solid, the three views (1), (2), (3) are given. Identify for each solid the corresponding top, front and side views.

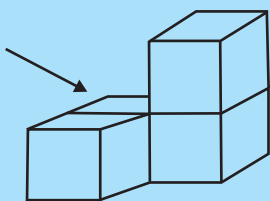
Solid	Its views		
	(1) 	(2) 	(3) 
			
 <p>5 Cubes</p>			
			

2. Draw a view of each solid as seen from the direction indicated by the arrow.

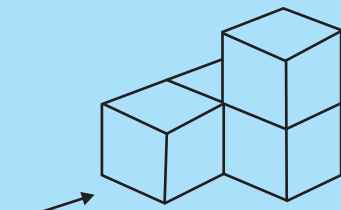




(i)



(ii)



(iii)

### WHAT HAVE WE DISCUSSED?

1. The circle, the square, the rectangle, the quadrilateral and the triangle are examples of **plane figures**; the cube, the cuboid, the sphere, the cylinder, the cone and the pyramid are examples of **solid shapes**.
2. Plane figures are of **two-dimensions (2-D)** and the solid shapes are of three-dimensions (**3-D**).
3. The corners of a solid shape are called its **vertices**; the line segments of its skeleton are its **edges**; and its flat surfaces are its **faces**.
4. A **net** is a skeleton-outline of a solid that can be folded to make it. The same solid can have several types of nets.
5. Solid shapes can be drawn on a flat surface (like paper) realistically. We call this **2-D representation of a 3-D solid**.
6. Two types of sketches of a solid are possible:
  - (a) An **oblique sketch** does not have proportional lengths. Still it conveys all important aspects of the appearance of the solid.
  - (b) An **isometric sketch** is drawn on an isometric dot paper, a sample of which is given at the end of this book. In an isometric sketch of the solid the measurements kept proportional.
7. **Visualising solid shapes** is a very useful skill. You should be able to see ‘hidden’ parts of the solid shape.
8. Different sections of a solid can be viewed in many ways:
  - (a) One way is to view by cutting or **slicing** the shape, which would result in the cross-section of the solid.
  - (b) Another way is by observing a 2-D **shadow** of a 3-D shape.
  - (c) A third way is to look at the shape from different angles; the **front-view**, the **side-view** and the **top-view** can provide a lot of information about the shape observed.

