CBSE NCERT Solutions for Class 11 Physics Chapter 2

Back of Chapter Questions

2.1 Fill in the blanks

(a) The volume of a cube of side 1 cm is equal to _____ m^3.

(b) The surface area of a solid cylinder of radius 2.0 cm and height 10.0 cm is equal to _____ $(mm)^2$

(c) A vehicle moving with a speed of 18 km h^{-1} covers_____ m in 1 s.

(d) The relative density of lead is 11.3. Its density is _____ g cm^{-3} or _____ kg m^{-3}.

Solution:

(a) 10^{-6}

The side of cube $= 1$ cm $= \frac{1}{100}$ m or 10^{-2} m
The volume of cube $= (10^{-2}$ m$)^3 = 10^{-6}$ m³

(b) 1.5×10^4

The surface area of a cylinder,
$A = 2\pi r^2 + 2\pi rh = 2\pi r(r + h)$
$= 2 \times 3.14 \times 2.0(12.0) = 150.7$ cm² $= 1.5 \times 10^4$ mm²
[In multiplication 2.0 has the minimum number of significant figures, which is 2. Hence the final answer should also have only 2 significant figures.]

(c) Using the conversion, 1 km/h $= \frac{5}{18}$ m/s

$18\frac{km}{h} = 18 \times \frac{5}{18}\frac{m}{s} = 5$ m/s

(d) Relative density $= \frac{\text{Density of substance}}{\text{Density of water}}$

The density of water $= 1$ g/cm³

The density of lead $=$ Relative density of lead $\times$ Density of water

$= 11.3 \times 1$ g/cm³ $= 11.3$ g/cm³

Again, 1 g $= 10^{-3}$ kg and 1 cm³ $= 10^{-6}$ m³

$\Rightarrow 1$g/cm³ $= \frac{10^{-3}}{10^{-6}}$ kg/m³ $= 10^3$ kg/m³

$\therefore 11.3$ g/cm³ $= 11.3 \times 10^3$ kg/m³

2.2. Fill in the blanks by suitable conversion of units

(a) $1 \text{ kg m}^2 \text{ s}^{-2} = \dots \text{g cm}^2 \text{ s}^{-2}$

(b) $1 \text{ m} = \dots \text{ly}$

(c) $3.0 \text{ m s}^{-2} = \dots \text{km h}^{-2}$

(d) $G = 6.67 \times 10^{-11} \text{ N m}^2 \text{ (kg)}^{-2} = \dots \text{(cm)}^3 \text{ s}^{-2} \text{ g}^{-1}$

Solution:

(a) $1 \text{ kg} = 10^3 \text{ g}$

$1 \text{ m}^2 = 10^4 \text{ cm}^2$

$1 \text{ kg m}^2 \text{ s}$

$-2 = 1 \text{ kg} \times 1 \text{ m}^2 \times 1 \text{ s}^{-2}$

$= 10^3 \text{ g} \times 10^4 \text{ cm}^2 \times 1 \text{ s}^{-2} = 10^7 \text{ g cm}^2 \text{ s}^{-2}$

(b)   A light year is a total distance travelled by light in one year.

$1 \text{ ly} = \text{Speed of light} \times \text{One year}$

$= (3 \times 10^8 \text{ m/s}) \times (365 \times 24 \times 60 \times 60 \text{ s})$

$= 9.46 \times 10^{15} \text{ m}$

$\therefore 1 \text{ m} = \dfrac{1}{9.46 \times 10^{15}} \text{ ly}$

(c) $1 \text{ m} = 10^{-3} \text{ km}$

Again, $1 \text{ s} = \frac{1}{3600} \text{ h}$

$1 \text{ s}^{-1} = 3600 \text{ h}^{-1}$

$1 \text{ s}^{-2} = (3600)^2 \text{ h}^{-2}$

$3 \text{ m s}^{-2} = (3 \times 10^{-3} \text{ km}) \times ((3600)^2 \text{ h}^{-2}) = 3.88 \times 10^{-4} \text{ km h}^{-2}$

(d) $1 \text{ N} = 1 \text{ kg m s}^{-2}$

$1 \text{ kg} = 10^{-3} \text{ g}^{-1}$

$1 \text{ m}^3 = 10^6 \text{ cm}^3$

$6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$

$= 6.67 \times 10^{-11} \times (1 \text{ kg m s}^{-2})(1 \text{ m}^2)(1 \text{ s}^{-2})$

$= 6.67 \times 10^{-11} \times (1 \text{ kg} \times 1 \text{ m}^3 \times 1 \text{ s}^{-2})$

$= 6.67 \times 10^{-11} \times (10^{-3} \text{ g}^{-1}) \times (10^6 \text{ cm}^3) \times (1 \text{ s}^{-2})$

$= 6.67 \times 10^{-8} \text{ cm}^3 \text{ s}^{-2} \text{ g}^{-1}$

2.3.   A calorie is a unit of heat or energy and it equals about 4.2 J. Where 1 J = 1 kg m^2 s^{-2}. Suppose we employ a system of units in which the unit of mass equals α kg, the unit of length equals β m, the unit of time is γ s. Show that a calorie has a magnitude 4.2 α^{-1} β^{-2} γ^2 in terms of the new units.

Solution:

Given:

1 calorie $= 4.2 \,(1 \text{ kg}) \,(1 \text{ m}^2) \,(1 \text{ s}^{-2})$

The new unit of mass = α kg

Hence, in terms of the new unit, $1 \text{ kg} = \frac{1}{\alpha} = \alpha^{-1}$

In terms of the new unit of length, $1 \text{ m} = \frac{1}{\beta} = \beta^{-1}$

$\Rightarrow 1 \text{ m}^2 = \beta^{-2}$

And, in terms of the new unit of time, $1 \text{ s} = \frac{1}{\gamma} = \gamma^{-1}$

$\Rightarrow 1 \text{ s}^{-2} = \gamma^2$

$\therefore 1 \text{ calorie} = 4.2 \,(\alpha^{-1})(\beta^{-2})(\gamma^2)$

2.4.   Explain this statement clearly: "To call a dimensional quantity 'large' or 'small' is meaningless without specifying a standard for comparison". In view of this, reframe the following statements wherever necessary:

(a)   atoms are very small objects

(b)   a jet plane moves with great speed

(c)   the mass of Jupiter is very large

(d)   the air inside this room contains a large number of molecules

(e)   a proton is much more massive than an electron

(f)   the speed of sound is much smaller than the speed of light.

Solution:

The given statement is true because a dimensionless quantity may be large or small in comparison to some standard reference. For example, the friction coefficient is dimensionless. The sliding friction coefficient is higher than the rolling friction coefficient but less than static friction.

(a)   An atom is a very small object in comparison to a basketball.

(b)   A jet plane moves with speed greater than that of a motorbike.

(c)   Mass of Jupiter is very large as compared to the mass of an elephant.

(d)   The air inside this room contains a large number of molecules as compared to that present in

(e)   A proton is more massive than an electron.

(f)   Speed of sound is less than the speed of light.

2.5.   A new unit of length is chosen such that the speed of light in vacuum is unity. What is the distance between the Sun and the Earth in terms of the new unit if light takes 8 min and 20 s to cover this distance?

Solution:

Distance between the Sun and the Earth:

= Speed of light × Time taken by light to cover the distance

Given that in the new unit, speed of light = 1 unit

Time taken, t = 8 min 20 s = 500 s

Distance between the Sun and the Earth $= 1 \times 500 = 500$ units

2.6.   Which of the following is the most precise device for measuring length:

(a)   a vernier callipers with 20 divisions on the sliding scale

(b)   a screw gauge of pitch 1 mm and 100 divisions on the circular scale

(c)   an optical instrument that can measure length to within a wavelength of light?

Solution:

A device with the minimum count is the most suitable to measure length.

Least count of vernier callipers

= 1 standard division (SD) – 1 vernier division (VD)

$1 - \dfrac{19}{20} = \dfrac{1}{20} = 0.05$ mm

Least count of screw gauge $= \dfrac{\text{pitch}}{\text{number of divisions}} = \dfrac{1}{100} = 0.01$ mm

Least count of an optical device = Wavelength of light $\sim$ 10–5 cm = 0.00001 cm

Hence, it can be inferred that an optical instrument is the most suitable device to measure length.

2.7.   A student measures the thickness of a human hair by looking at it through a microscope of magnification 100. He makes 20 observations and finds that the average width of the hair in the field of view of the microscope is 3.5 mm. What is the estimate on the thickness of hair?

Solution:

Magnification of the microscope $= 100$

The average width of the hair in the field of view of the microscope $=$ 3.5 mm

$\therefore$ The actual thickness of the hair is $= \frac{3.5}{100} =$ 0.035 mm.

2.8. Answer the following:

(a) You are given a thread and a metre scale. How will you estimate the diameter of the thread?

(b) A screw gauge has a pitch of 1.0 mm and 200 divisions on the circular scale. Do you think it is possible to increase the accuracy of the screw gauge arbitrarily by increasing the number of divisions on the circular scale?

(c) The mean diameter of a thin brass rod is to be measured by vernier callipers. Why is a set of 100 measurements of the diameter expected to yield a more reliable estimate than a set of 5 measurements only?

Solution:

(a) Wrap the thread on a uniform, smooth rod in such a way that the coils thus formed are very close to each other. Measure the length of the thread using a metre scale. The diameter of the thread is given by the relation,

$$\text{Diameter} = \frac{\text{length of thread}}{\text{Number of turns}}$$

(b) It is not possible to increase the accuracy of a screw gauge by increasing the number of divisions of the circular scale. Increasing the number of divisions of the circular scale will increase its accuracy to a certain extent only.

(c) A set of 100 measurements is more reliable than a set of 5 measurements because random errors involved in the former are very less as compared to the latter.

2.9. The photograph of a house occupies an area of 1.75 cm^2 on a 35 mm slide. The slide is projected on to a screen, and the area of the house on the screen is 1.55 m^2. What is the linear magnification of the projector-screen arrangement.

Solution:

Area of the house on the slide $=$ 1.75 cm$^2 =$ 1.75×10^{-4} m^2

Area of the image of the house formed on the screen $=$ 1.55 m^2

Arial magnification, $= \frac{\text{Area of image}}{\text{Area of object}} = \frac{1.55}{1.75 \times 10^{-4}} = 0.89 \times 10^4$

$\therefore$ Linear magnification $= \sqrt{\text{Arial magnification}} = \sqrt{0.89 \times 10^4} = 94.11$

2.10. State the number of significant figures in the following:

(a) 0.007 m^2

(b) 2.64×10^{24} kg

(c)   0.2370 g cm^{-3}

(d)   6.320 J

(e)   6.032 N m^{-2}

(f)   0.0006032 m^2

Solution:

(a)   The number of significant figures in 0.007 m^2 is 1.

    If the number is less than one, then all zeros on the right of the decimal point (but left to the first non-zero) are insignificant. This means that here, two zeros after the decimal are not significant. Hence, only 7 is a significant figure in this quantity.

(b)   The number of significant figures in 2.64 $\times 10^{24}$ kg is 3.

    Here, the power of 10 is irrelevant for the determination of significant figures. Hence, all digits i.e., 2, 6 and 4 are significant figures.

(c)   The number of significant figures in 0.2370 g cm^{-3} is 4.

    For a number with decimals, the trailing zeroes are significant. Hence, besides digits 2, 3 and 7, 0 that appears after the decimal point is also a significant figure.

(d)   The number of significant figures in 6.320 J is 4.

    For a number with decimals, the trailing zeroes are significant. Hence, all four digits appearing in the given quantity are significant figures.

(e)   The number of significant figures in 6.032 N m^{-2} is 4.

    All zeroes between two non-zero digits are always significant.

(f)   The number of significant figures in 0.0006032 m^2 is 4.

    If the number is less than one, then the zeroes on the right of the decimal point (but left to the first non-zero) are insignificant. Hence, all three zeroes appearing before 6 are not significant figures. All zeros between two non-zero digits are always significant. Hence, the remaining four digits are significant figures.

2.11.   The length, breadth and thickness of a rectangular sheet of metal are 4.234 m, 1.005 m, and 2.01 cm respectively. Give the area and volume of the sheet to correct significant figures.

Solution:

Given:

Length of the sheet, $l = 4.234$ m

The breadth of the sheet, $b = 1.005$ m

Thickness of sheet, $h = 2.01$ cm $= 0.0201$ m

Hence, area and volume both must have least significant figures i.e., 3.

Surface area of the sheet $= 2 (l \times b + b \times h + h \times l)$

$= 2(4.234 \times 1.005 + 1.005 \times 0.0201 + 0.0201 \times 4.234)$

$= 2 (4.25517 + 0.02620 + 0.08510)$

$= 2 \times 4.360$

$= 8.72 \text{ m}^2$

Volume of the sheet $= l \times b \times h$

$= 4.234 \times 1.005 \times 0.0201$

$= 0.0855 \text{ m}^3$

This number has only 3 significant figures i.e., 8, 5, and 5.

2.12. The mass of a box measured by a grocer's balance is 2.300 kg. Two gold pieces of masses 20.15 g and 20.17 g are added to the box. What is (a) the total mass of the box, (b) the difference in the masses of the pieces to correct significant figures?

Solution:

Given:

Mass of grocer's box $= 2.300 \text{ kg}$

Mass of gold piece I $= 20.15 \text{ g} = 0.02015 \text{ kg}$

Mass of gold piece II $= 20.17 \text{ g} = 0.02017 \text{ kg}$

(a)   Total mass of the box $= 2.3 + 0.02015 + 0.02017 = 2.34032 \text{ kg}$

In addition, the final result should retain as many decimal places as there are in the number with the least decimal places. Hence, the total mass of the box is 2.3 kg.

(b)   Difference in masses $= 20.17 - 20.15 = 0.02 \text{ g}$

In subtraction, the final result should retain as many decimal places as there are in the number with the least decimal places.

2.13. A physical quantity P is related to four observables a, b, c and d as follows:

$P = a^3 b^2 / \sqrt{c} d$

The percentage errors of measurement in a, b, c and d are 1%, 3%, 4% and 2%, respectively. What is the percentage error in the quantity P? If the value of P calculated using the above relation turns out to be 3.763, to what value should you round off the result?

Solution:

Given:

$P = a^3 b^2 / \sqrt{c}d$

$$\frac{\Delta P}{P} = \frac{3\Delta a}{a} + \frac{2\Delta b}{b} + \frac{1}{2}\frac{\Delta c}{c} + \frac{\Delta d}{d}$$

$$\frac{\Delta P}{P} \times 100 = 3\frac{\Delta a}{a} \times 100 + 2\frac{\Delta b}{b} \times 100 + \frac{1}{2}\frac{\Delta c}{c} \times 100 + \frac{\Delta d}{d} \times 100$$

The percentage error in P $= 3 \times 1 + 2 \times 3 + \frac{1}{2} \times 4 + 2 = 13\%$

Value of P is given as 3.763.

By rounding off the given value to the first decimal place, we get P = 3.8.

2.14. A book with many printing errors contains four different formulas for the displacement y of a particle undergoing a certain periodic motion:

(a) $y = a \sin 2\pi\, t/T$

(b) $y = a \sin vt$

(c) $y = \left(\frac{a}{T}\right) \sin t/a$

(d) $y = \left(a\sqrt{2}\right)(\sin 2\pi\, t/T + \cos 2\pi\, t/T)$

(a = maximum displacement of the particle, v = speed of the particle. T = time-period of motion). Rule out the wrong formulas on dimensional grounds.

Solution:

(a) $y = a \sin 2\pi\, t/T$ is dimensionally correct.

       Dimension of $y = M^0\, L^1\, T^0$

       Dimension of $a = M^0\, L^1\, T^0$

       Dimension of $= M^0\, L^0\, T^0$

       Dimension of L.H.S = Dimension of R.H.S

       Hence, the given formula is dimensionally correct.

(b) $y = a \sin vt$ is dimensionally incorrect

       Dimension of $y = M^0\, L^1\, T^0$

       Dimension of $a = M^0\, L^1\, T^0$

       Dimension of $vt = M^0\, L^1\, T^{-1} \times M^0\, L^0\, T^1 = M^0\, L^1\, T^0$

       But the argument of the trigonometric function must be dimensionless, which is not so in the given case. Hence, the given formula is dimensionally incorrect.

(c) $y = \left(\frac{a}{T}\right) \sin t/a$ is dimensionally Incorrect

       Dimension of $y = M^0 L^1 T^0$

Dimension of $a/T = M^0 L^1 T^{-1}$

Dimension of $t/a = M^0 L^{-1} T^1$

But the argument of the trigonometric function must be dimensionless, which is not so in the given case. Hence, the formula is dimensionally incorrect.

(d)　　$y = (a\sqrt{2})(\sin 2\pi\, t/T + \cos 2\pi\, t/T)$ is dimensionally correct.

Dimension of $y = M^0\, L1\, T0$

Dimension of $a = M^0\, L^1\, T^0$

Dimension of $t/T = M^0\, L^0\, T^0$

Since the argument of the trigonometric function must be dimensionless (which is true in the given case), the dimensions of y and a are the same. Hence, the given formula is dimensionally correct.

2.15.　A famous relation in physics relates 'moving mass' m to the 'rest mass' mo of a particle in terms of its speed v and the speed of light, c. (This relation first arose as a consequence of special relativity due to Albert Einstein). A boy recalls the relation almost correctly but forgets where to put the constant c. He writes:

$$m = \frac{m_0}{(1 - v^2)^{1/2}}$$

Guess where to put the missing c.

Solution:

Dimension of $m = M^1\, L^0\, T^0$

Dimension of $v = M^0\, L^1\, T^{-1}$

Dimension of $v^2 = M^0\, L^2\, T^{-2}$

Dimension of $c = M^0\, L^1\, T^{-1}$

The given formula will be dimensionally correct only when the dimension of L.H.S is the same as that of R.H.S. This is only possible when the factor, $(1 - v^2)^{1/2}$ is dimensionless i.e., $(1 - v^2)$ is dimensionless. This is only possible if v^2 is divided by c^2. Hence, the correct relation is

$$m = \frac{m_0}{\left(1 - \dfrac{v^2}{c^2}\right)^{1/2}}$$

2.16.　The unit of length convenient on the atomic scale is known as an angstrom and is denoted by Å: 1 Å $= 10^{-10}$ m. The size of a hydrogen atom is about 0.5 Å. What is the total atomic volume in m^3 of a mole of hydrogen atoms?

Solution:

Radius of hydrogen atom, $r = 0.5$ Å $= 0.5 \times 10^{-10}$ m

Volume of hydrogen atom $= \frac{4}{3}\pi r^3 = \frac{4}{3} \times \frac{22}{7} \times (0.5 \times 10^{-10})^3 = 0.524 \times 10^{-30}$ m³

1 mole of hydrogen contains 6.023×10^{23} hydrogen atoms.

Volume of 1 mole of hydrogen atoms $= 6.023 \times 10^{23} \times 0.524 \times 10^{-30}$

$$= 3.16 \times 10^{-7} \text{ m}^3$$

2.17. One mole of an ideal gas at standard temperature and pressure occupies 22.4 L (molar volume). What is the ratio of molar volume to the atomic volume of a mole of hydrogen? (Take the size of hydrogen molecule to be about 1 Å). Why is this ratio so large?

Solution:

Given:

Size of hydrogen atom (diameter) $= 1$ Å

Radius of hydrogen atom, r $= 0.5$ Å $= 0.5 \times 10^{-10}$ m

Volume of hydrogen atom $= \frac{4}{3}\pi r^3 = \frac{4}{3} \times \frac{22}{7} \times (0.5 \times 10^{-10})^3 = 0.524 \times 10^{-30}$ m³

1 mole of hydrogen contains 6.023×10^{23} hydrogen atoms.

Volume of 1 mole of hydrogen atoms $V_a = 6.023 \times 10^{23} \times 0.524 \times 10^{-30}$

$= 3.16 \times 10^{-7}$ m³

Molar volume of 1 mole of hydrogen atoms at STP, $V_m = 22.4$ L $= 22.4 \times 10^{-3}$ m³

$$\therefore \frac{V_m}{V_a} = \frac{22.4 \times 10^{-3}}{3.16 \times 10^{-7}} = 7.08 \times 10^4$$

2.18. Explain this common observation clearly: If you look out of the window of a fast moving train, the nearby trees, houses etc. seem to move rapidly in a direction opposite to the train's motion, but the distant objects (hilltops, the Moon, the stars etc.) seem to be stationary. (In fact, since you are aware that you are moving, these distant objects seem to move with you).

Solution:

Line of sight is defined as an imaginary line that joins an object with the eye of an observer. When we look at neighbouring stationary objects like trees, houses, etc.

While sitting in a moving train, they appear to move rapidly in the opposite direction because the line of sight changes very rapidly. On the other hand, distant objects such as trees, stars, etc. appear stationary because of the large distance. As a result, the line of sight does not change its direction rapidly.

2.19. The principle of 'parallax' in section 2.3.1 is used in the determination of distances of very distant stars. The baseline AB is the line joining the Earth's two locations six months apart in its orbit around the Sun. That is, the baseline is about the diameter of the Earth's orbit $\approx 3 \times 1011$m. However, even the nearest stars are so distant that

with such a long baseline, they show parallax only of the order of 1" (second) of arc or so. A parsec is a convenient unit of length on the astronomical scale. It is the distance of an object that will show a parallax of 1" (second) of arc from opposite ends of a baseline equal to the distance from the Earth to the Sun. How much is a parsec in terms of metres?

Solution:

Diameter of Earth's orbit $= 3 \times 10^{11}$ m

Radius of Earth's orbit, r $= 1.5 \times 10^{11}$ m

Let the distance parallax angle be $1'' = 4.847 \times 10^{-6}$ rad.

Let the distance of the star be D.

Parsec is defined as the distance at which the average radius of the Earth's orbit subtends an angle of 1" (second).

We have $\theta = \frac{r}{D}$

$$\Rightarrow D = \frac{r}{\theta} = \frac{1.5 \times 10^{11}}{4.847 \times 10^{-6}} \approx 3.09 \times 10^{16} \text{ m}$$

Hence, 1 parsec $\approx 3.09 \times 10^{16}$ m

2.20. The nearest star to our solar system is 4.29 light years away. How much is this distance in terms of parsecs? How much parallax would this star (named Alpha Centauri) show when viewed from two locations of the Earth six months apart in its orbit around the Sun?

Solution:

Distance of the star from the solar system = 4.29 light years

1 light year is the distance travelled by light in one year.

1 light year = Speed of light $\times$ 1 year

$= 3 \times 10^8 \times 365 \times 24 \times 60 \times 60 = 94608 \times 10^{11}$ m

$\therefore$ 4.29 light years $= 405868.32 \times 10^{11}$ m

And 1 parsec $= 3.08 \times 10^{16}$ m

$\because$ 4.29 light year $= \dfrac{4.059 \times 10^{16}}{3.08 \times 10^{16}} = 1.32$ parsec

Now, $\theta = \frac{d}{D}$

Where

d is the diameter of earth $= 3 \times 10^{11}$ m

D is the distance of the star from the solar system $= 405868.32 \times 10^{11}$ m

$$\therefore \theta = \frac{3 \times 10^{11}}{405868.32 \times 10^{11}} = 7.39 \times 10^{-6} \text{ rad}$$

$$\therefore 1" = 4.847 \times 10^{-6} \text{ rad}$$

$$\Rightarrow \theta = \frac{7.39 \times 10^{-6}}{4.847 \times 10^{-6}} = 1.52''$$

2.21. Precise measurements of physical quantities are a need of science. For example, to ascertain the speed of an aircraft, one must have an accurate method to find its positions at closely separated instants of time. This was the actual motivation behind the discovery of radar in World War II. Think of different examples in modern science where precise measurements of length, time, mass etc. are needed. Also, wherever you can, give a quantitative idea of the precision needed.

Solution:

Yes, it is very true that accurate physical quantity measurements are crucial for the development of science. For example, ultra-shot laser pulses (time interval $\sim$ 10–15 s) are used to measure time intervals in several physical and chemical processes.

X-ray spectroscopy is used to determine the inter-atomic separation or inter-planer spacing.

Mass spectrometer development makes it possible to accurately measure the mass of electrons.

2.22. Just as precise measurements are necessary in science, it is equally important to be able to make rough estimates of quantities using rudimentary ideas and common observations. Think of ways by which you can estimate the following (where an estimate is difficult to obtain, try to get an upper bound on the quantity):

(a) the total mass of rain-bearing clouds over India during the Monsoon

(b) the mass of an elephant

(c) the wind speed during a storm

(d) the number of strands of hair on your head

(e) the number of air molecules in your classroom.

Solution:

(a) During monsoons, a meteorologist records about 200 cm of rainfall in India i.e., the height of water column, h = 200 cm = 2.00 m

Area of country, A = 3.3×10^{12} m^2

Hence, volume of rainwater, V = A $\times$ h = 6.6×10^{12} m

Density of water, ρ = 1×10^3 kg m^{-3}

Hence, mass of rainwater = $\rho \times$ V = 6.6×10^{15} kg

Hence, the total mass of rain-bearing clouds over India is approximately 6.6×10^{15} kg.

(b)   Consider a ship of known base area floating in the sea. Measure its depth in the sea (say d_1).

Volume of water displaced by the ship, $V_b = A d_1$

Now, move an elephant on the ship and measure the depth of the ship (d_2) in this case.

Volume of water displaced by the ship with the elephant on board, $V_{be} = A d_2$

Volume of water displaced by the elephant $= A d_2 - A d_1$

Density of water $= D$

Mass of elephant $= AD (d_2 - d_1)$

(c)   Wind speed during a storm can be measured by an anemometer. As the wind blows, it rotates.

The rotation made by the anemometer in one second gives the value of wind speed.

Area of the head surface carrying hair $= A$

(d)   With the help of a screw gauge, the diameter and hence, the radius of a hair can be

determined. Let it be r.

Area of one hair $= \pi r^2$

Number of strands of hair $= \dfrac{\text{total surface area}}{\text{area of one hair}} = \dfrac{A}{\pi r^2}$

(e)   Let the volume of the room be V.

One mole of air at NTP occupies $22.4\ l$ i.e., 22.4×10^{-3} m^3 volume.

Number of molecules in one mole $= 6.023 \times 10^{23}$

Number of molecules in the room of volume V $= \dfrac{6.023 \times 10^{23}}{22.4 \times 10^{-3}} \times V = 1.35 \times 10^{28} V$

2.23.   The Sun is a hot plasma (ionized matter) with its inner core at a temperature exceeding 10^7 K, and its outer surface at a temperature of about 6000 K. At these high temperatures, no substance remains in a solid or liquid phase. In what range do you expect the mass density of the Sun to be, in the range of densities of solids and liquids or gases? Check if your guess is correct from the following data: mass of the Sun $= 2.0 \times 10^{30}$ kg, radius of the Sun $= 7.0 \times 10^8$ m.

Solution:

Mass of the Sun, $M = 2.0 \times 10^{30}$ kg

Radius of the Sun, $R = 7.0 \times 10^8$ m

Volume of the Sun, $V = \frac{4}{3}\pi R^2 = \frac{4}{3} \times 3.14 \times (7.0 \times 10^8)^3 = 1.44 \times 10^{27}$ m^3

Density of the Sun $= \frac{mass}{volume} = \frac{2.0 \times 10^{30} \, kg}{1.44 \times 10^{27} \, m^3} = 1.39 \times 10^3$ kg/m^3

The density of the Sun is in the density range of solids and liquids. This high density is attributed to the intense gravitational attraction of the inner layers on the outer layer of the Sun.

2.24. When the planet Jupiter is at a distance of 824.7 million kilometers from the Earth, its angular diameter is measured to be 35.72" of arc. Calculate the diameter of Jupiter.

Solution:

Distance of Jupiter from the Earth, D $= 824.7 \times 10^6$ km $= 824.7 \times 10^9$ m

Angular diameter $= 35.72" = 35.72 \times 4.874 \times 10^{-6}$ rad $= 1.74 \times 10^{-4}$ rad

Let the diameter of Jupiter $= d$

Using the relation, $\theta = \frac{d}{D}$

$\Rightarrow d = D\theta = 824.7 \times 10^9 \times 1.74 \times 10^{-4} = 1.44 \times 10^8$ m or 1.44×10^5 km

Additional Exercises

2.25. A man walking briskly in rain with speed v must slant his umbrella forward making an angle θ with the vertical. A student derives the following relation between θ and v: tan $\theta = v$ and checks that the relation has a correct limit: as $v \to 0$, $\theta \to 0$, as expected. (We are assuming there is no strong wind and that the rain falls vertically for a stationary man). Do you think this relation can be correct? If not, guess the correct relation.

Solution:

Incorrect by dimensions

The relation is tan $\theta = v$

Dimension of R.H.S $= M^0 \, L^1 \, T^{-1}$

Dimension of L.H.S $= M^0 \, L^0 \, T^0$ ($\because$The trigonometric function is considered to be a dimensionless quantity)

Dimension of R.H.S is not equal to the dimension of L.H.S. Hence, the given relation is not correct dimensionally.

To make the given relation correct, the R.H.S should also be dimensionless. One way to achieve this is by dividing the R.H.S by the speed of rainfall v'.

Therefore, the relation reduces to tan $\theta = \frac{v}{v'}$

This relation is dimensionally correct.

2.26. It is claimed that two cesium clocks, if allowed to run for 100 years, free from any disturbance, may differ by only about 0.02 s. What does this imply for the accuracy of the standard cesium clock in measuring a time-interval of 1 s?

Solution:

Difference in time of caesium clocks $=$ 0.02 s

Time taken for the difference $=$ 100 years

$= 100 \times 365 \times 24 \times 60 \times 60 = 3.15 \times 10^9$ s

In 3.15×10^9 s, the caesium clock shows a time difference of 0.02 s.

In 1s, the clock will show a time difference of $\frac{0.02}{3.15 \times 10^9}$ s.

Hence, the accuracy of a standard caesium clock in measuring a time interval of 1 s is

$$\frac{3.15 \times 10^9}{0.02} = 157.5 \times 10^9 \text{ s} = 1.5 \times 10^{11} \text{ s}$$

2.27. Estimate the average mass density of a sodium atom assuming its size to be about 2.5 Å. (Use the known values of Avogadro's number and the atomic mass of sodium). Compare it with the density of sodium in its crystalline phase: 970 kg m^{-3}. Are the two densities of the same order of magnitude? If so, why?

Solution:

Diameter of sodium atom = Size of sodium atom $=$ 2.5 Å

Radius of sodium atom, $r = \frac{1}{2} \times 2.5 \text{ Å} = 1.25 \text{ Å} = 1.25 \times 10^{-10}$ m

Volume of sodium atom, $V = \frac{4}{3} \pi r^3 = \frac{4}{3} \times 3.14 \times (1.25 \times 10^{-10})^3 \text{ m}^3 = 8.18 \times 10^{-30} \text{ m}^3$

According to the Avogadro hypothesis, one mole of sodium contains 6.023×10^{23} atoms and has a mass of 23 g or 23×10^{-3} kg.

$\therefore$ Mass of one atom $= \frac{23 \times 10^{-3}}{6.023 \times 10^{23}} \text{ kg} = 3.82 \times 10^{-26}$ kg

Density of sodium atom, $\rho = \frac{3.82 \times 10^{-26} \text{ kg}}{8.18 \times 10^{-30} \text{ m}^3} = 4.67 \times 10^3 \text{ kg/m}^3$

It is given that the density of sodium in crystalline phase is 970 kg m^{-3}.

Hence, the density of sodium atom and the density of sodium in its crystalline phase are not in the same order. This is because in solid phase, atoms are closely packed. Thus, the inter-atomic separation is very small in the crystalline phase.

2.28. The unit of length convenient on the nuclear scale is a fermi: $1 \text{ f} = 10^{-15}$ m. Nuclear sizes obey roughly the following empirical relation: $r = r_0 A^{\frac{1}{3}}$ where r is the radius of the nucleus, A its mass number, and ro is a constant equal to about, 1.2 f. Show that the

rule implies that nuclear mass density is nearly constant for different nuclei. Estimate the mass density of sodium nucleus. Compare it with the average mass density of a sodium atom obtained in Exercise. 2.27.

Solution:

Radius of nucleus r is given by the relation,

$r = r_0 A^{\frac{1}{3}}$ … (i)

$r_0 = 1.2\, f = 1.2 \times 10^{-15}\, m$

Volume of nucleus, $V = \frac{4}{3}\pi r^3$

$= \frac{4}{3}\pi \left(r_0 A^{\frac{1}{3}} \right)^3 = \frac{4}{3}\pi r_0^3 A$ ......(ii)

Now, the mass of a nuclei M is equal to its mass number i.e.,

$M = A\, amu = A \times 1.66 \times 10^{-27}\, kg$

The density of the nucleus,

$\rho = \dfrac{\text{Mass of nucleus}}{\text{Volume of nucleus}} = \dfrac{A \times 1.66 \times 10^{-27}}{\frac{4}{3}\pi r_0^3 A} = \dfrac{1.245}{\pi r_0^3} \times 10^{-27}\, kg/m^3$

This relation shows that nuclear mass depends only on constant r_0. Hence, the nuclear mass densities of all nuclei are nearly the same.

The density of the sodium nucleus is given by,

$\rho_{\text{Sodium}} = \dfrac{1.245}{\pi(1.2 \times 10^{-15})^3} \times 10^{-27}\, \dfrac{kg}{m^3} = 2.3 \times 10^{17}\, kg/m^3$

2.29. A LASER is a source of very intense, monochromatic, and unidirectional beam of light. These properties of a laser light can be exploited to measure long distances. The distance of the Moon from the Earth has been already determined very precisely using a laser as a source of light. A laser light beamed at the Moon takes 2.56 s to return after reflection at the Moon's surface. How much is the radius of the lunar orbit around the Earth?

Solution:

Time taken by the laser beam to return to Earth after reflection from the Moon $= 2.56\, s$

Speed of light $= 3 \times 10^8\, m/s$

Time taken by the laser beam to reach Moon $= 2.56 \times \frac{1}{2} = 1.28\, s$

The radius of the lunar orbit $=$ Distance between the Earth and the Moon

$= 1.28 \times 3 \times 10^8 = 3.84 \times 10^8\, m = 3.84 \times 10^5\, km$

2.30. A SONAR (sound navigation and ranging) uses ultrasonic waves to detect and locate objects under water. In a submarine equipped with a SONAR the time delay between generation of a probe wave and the reception of its echo after reflection from an enemy submarine is found to be 77.0 s. What is the distance of the enemy submarine? (Speed of sound in water $=$ 1450 m s^{-1}).

Solution:

Let the distance between the ship and the enemy submarine be 'S'.

Speed of sound in water $=$ 1450 m/s

Time lag between transmission and reception of Sonar waves $=$ 77 s

In this time lag, sound waves travel a distance which is twice the distance between the ship and the submarine (2S).

Time taken for the sound to reach the submarine $= \frac{1}{2} \times 77 = 38.5$ s

$\therefore$ Distance between the ship and the submarine (S)

$= 1450 \times 38.5 = 55825$ m $= 55.8$ km

2.31. The farthest objects in our Universe discovered by modern astronomers are so distant that light emitted by them takes billions of years to reach the Earth. These objects (known as quasars) have many puzzling features, which have not yet been satisfactorily explained. What is the distance in km of a quasar from which light takes 3.0 billion years to reach us?

Solution:

Time taken by quasar light to reach Earth $= 3$ billion years

$= 3 \times 10^9$ years

$= 3 \times 10^9 \times 365 \times 24 \times 60 \times 60$ s

Speed of light $= 3 \times 10^8$ m/s

Distance between the Earth and quasar

$= (3 \times 10^8) \times (3 \times 10^9 \times 365 \times 24 \times 60 \times 60)$

$= 283824 \times 10^{20}$ m

$= 2.8 \times 10^{22}$ km

2.32. It is a well known fact that during a total solar eclipse the disk of the moon almost completely covers the disk of the Sun. From this fact and from the information you can gather from examples 2.3 and 2.4, determine the approximate diameter of the moon.

Solution:

The position of the Sun, Moon, and Earth during a lunar eclipse is shown in the given figure.
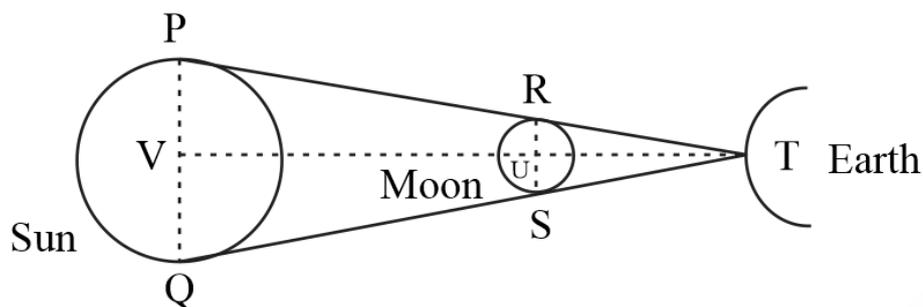
Distance of the Moon from the Earth $= 3.84 \times 10^8$ m

Distance of the Sun from the Earth $= 1.496 \times 10^{11}$ m

Diameter of the Sun $= 1.39 \times 10^9$ m

It can be observed that ΔTRS and ΔTPQ are similar. Hence, it can be written as:

$$\frac{PQ}{RS} = \frac{VT}{UT}$$

$$\Rightarrow \frac{1.39 \times 10^9}{RS} = \frac{1.496 \times 10^{11}}{3.84 \times 10^8}$$

$$RS = \frac{1.39 \times 10^9 \times 3.84 \times 10^8}{1.496 \times 10^{11}} = 3.57 \times 10^6 \text{ m}$$

Hence, the diameter of the Moon is 3.57×10^6 m.

2.33. A great physicist of this century (P.A.M. Dirac) loved playing with numerical values of Fundamental constants of nature. This led him to an interesting observation. Dirac found that from the basic constants of atomic physics (c, e, mass of electron, mass of proton) and the gravitational constant G, he could arrive at a number with the dimension of time. Further, it was a very large number, its magnitude being close to the present estimate on the age of the universe (~15 billion years). From the table of fundamental constants in this book, try to see if you too can construct this number (or any other interesting number you can think of). If its coincidence with the age of the universe were significant, what would this imply for the constancy of fundamental constants?

Solution:

One relation consists of some fundamental constants that give the age of the Universe by:

$$t = \left(\frac{e^2}{4\pi\varepsilon_0} \right)^2 \times \left(\frac{1}{m_p m_e^2 \, c^3 G} \right)$$

Where,

t $=$ Age of Universe

e $=$ Charge of electrons $= 1.6 \times 10^{-19}$ C

$\varepsilon_0 =$ Absolute permittivity

m_p = Mass of protons = 1.67×10^{-27} kg

m_e = Mass of electrons = 9.1×10^{-31} kg

c = Speed of light = 3×10^8 m/s

G = Universal gravitational constant = 6.67×10^{-11} N m^2 kg^{-2}

Also $1/4\pi\varepsilon_0$ = 9×10^9 N m^2/C^2

Substituting these values in the equation, we get

$$t = \left(\frac{(9 \times 10^9 \times (1.6 \times 10^{-19})^2)^2}{1.67 \times 10^{-27} \times (9.1 \times 10^{-31})^2 \times (3 \times 10^8)^3 \times 6.67 \times 10^{-11}} \right)$$
$$= 2.13 \times 10^{16} \text{ s}$$

$= 6.7542 \times 10^8$ years